



**ANALYSIS OF A VAN DE GRAAFF GENERATOR FOR EMP
DIRECT CURRENT SURVIVABILITY TESTING**

THESIS

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AFIT-ENP-13-M-39

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SURVIVABILITY TESTING

THESIS

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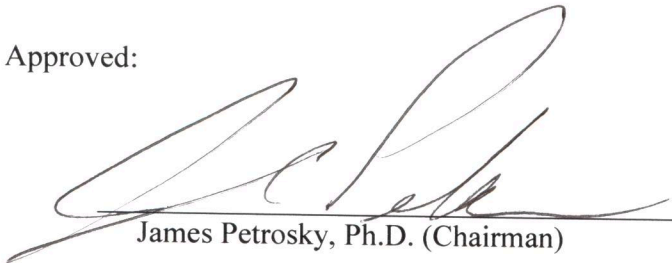
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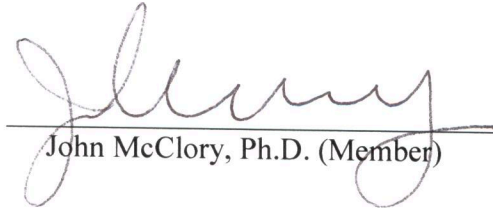
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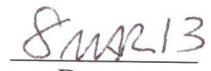
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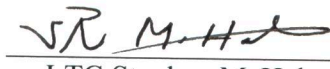
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ABSTRACT

The direct current produced from the Van de Graaff (VDG) at the Air Force Research Laboratory (AFRL) has been measured and analyzed. The current pulse produced from the VDG is oscillatory. Experimental data show complete damping occurs after 8 oscillations and within 10^{-6} seconds. The spark gap distance and circuit resistance were varied to determine if the circuit could convert to an overdamped RLC circuit in order to reduce the oscillations. The data establishes that the VDG produces at least 3 full wave Fourier frequencies of: 3, 7, and 15 MHz \pm 2.0 MHz, while the first oscillation had a measured mean frequencies of: 8.56 MHz \pm 0.4 MHz for the 3" spark gap distance; 6" had a measured frequency of 13.95 MHz \pm 1.0 MHz, and finally 7" had a measured value of 15.78 MHz \pm 1.3 MHz. The direct current amplitude of the first oscillation also rose as a function of spark gap distance from 202 ± 13.82 (A) at a spark gap of 3" to 354 ± 22.10 (A) for a spark gap of 8". Using the settings explored in this thesis, the VDG has some value for use in preliminary Electromagnetic Pulse (EMP) direct current testing, but further research is required in order for it to meet MIL-STD-464 validation criteria.

Acknowledgments

I would like to express my sincere appreciation to my faculty advisor, Dr. James Petrosky, for his guidance and support throughout the course of this thesis. His insight and experience were certainly appreciated. I would also like to thank my sponsor, Dr. Dean Evans, from the Air Force Research Laboratory for helping me to obtain the material, location and work force necessary to safely run and operate the Van de Graaff (VDG) generator. I would also like to thank Dr. Sergey Basun and Dr. Carl Liebig from the Air Force Research Laboratory for working with me during the long arduous hours of research with the VDG. I also give the same gratitude for Dr. Ashley Francis from AFIT who also participated in the VDG experiments. I would also like to thank LTC Steve McHale and Dr. John McClory for their listening ear and guidance throughout.

This has taken a lot of time away from my family. I would like to extend my love and thanks to my best friend (my beautiful wife). She has stood beside me through it all, and I plan on being there for her to the very end. My children are the delight of my life. May I always find the time to kick the soccer ball, throw the football, and play with you at all times. Love Dad.

LTC Robert J. Kress

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ANALYSIS OF A VAN DE GRAAFF GENERATOR FOR EMP DIRECT CURRENT SURVIVABILITY TESTING

CHAPTER 1

INTRODUCTION

1.1 Background

The rate of change of the electric and magnetic fields of an electromagnetic pulse (EMP) event are a threat to electronic equipment. Equipment that performs critical, time-urgent command, control, communications, computer, and intelligence (C⁴I) missions must be hardened to operate through EMP events without damage or functional upsets. Survivable C⁴I capabilities are essential to a credible military deterrent [1].

As with conventional weapons, nuclear weapon use is typically associated with the blast, shock, and thermal effects. Additional effects, such as prompt radiation, fallout, and EMP are less well understood and need additional study and experimental analysis [2]. Therefore, the Van de Graaff (VDG) at the Air Force Research Laboratory (AFRL) has been measured and analyzed for future use in EMP direct current survivability testing and EMP educational benefit.

An abrupt pulse of electromagnetic radiation usually results from certain types of high energy explosions, especially a nuclear explosion, or from a suddenly fluctuating magnetic field. The resulting rapidly-changing electric and magnetic fields can couple with electrical/electronic systems to produce damaging current and voltage surges.

The Department of Defense has established “Electromagnetic Environmental Effects Requirements for Systems” as described in “MIL STD 464” [3]. In Section 5.5 of

MIL STD 464, it gives the parameters established to survive an EMP. The requirements are: “The system shall meet its operational performance requirements after being subjected to the EMP environment. If an EMP environment is not defined by the procuring activity, Figure 1 shall be used. This requirement is not applicable unless otherwise specified by the procuring activity. Compliance shall be verified by system, subsystem, and equipment level experiments, analysis, or a combination thereof.” [3].

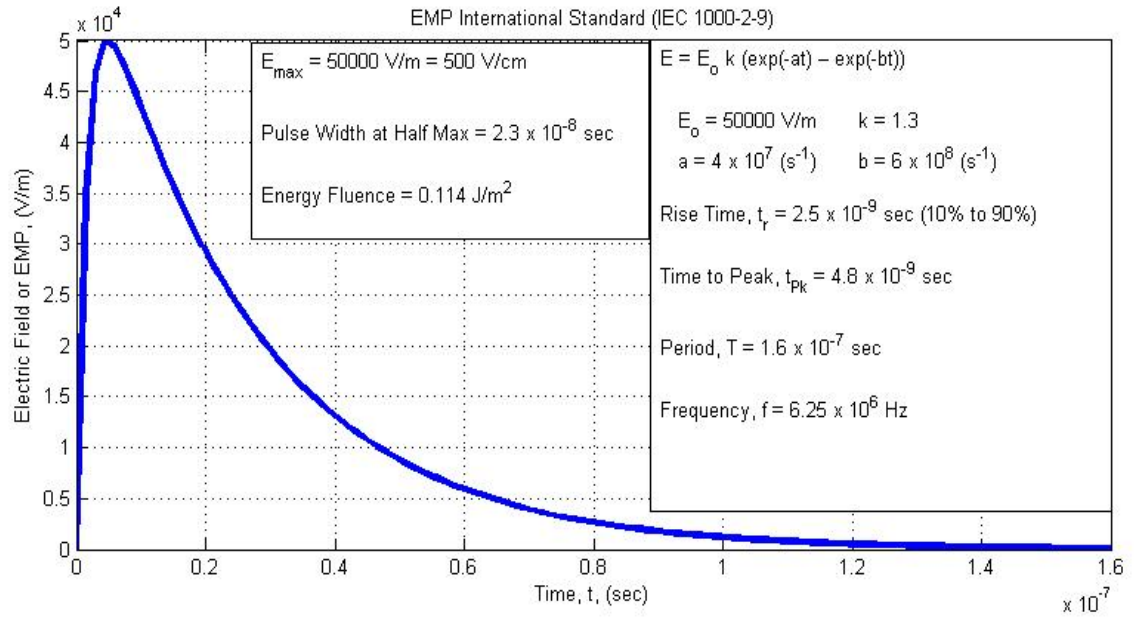


Figure 1. The MIL-STD-464 default model of a free-field EMP environment is shown. The EMP electric field is shown as a function of time [3].

This waveform conforms to the model equation, as shown in Equation (1):

$$E(t) = E_o k (e^{-at/\tau} - e^{-bt/\tau}) = E_o k (e^{-at} - e^{-bt}), \quad (1)$$

where $E_o = 50000$ (V/m), $\alpha = a/\tau = 4 \times 10^7 \text{ s}^{-1}$, $\beta = b/\tau = 6 \times 10^8 \text{ s}^{-1}$, $k = 1.3$ and $\tau = 0.258 \text{ s}$ [4].

1.2 Problem Statement and Purpose

The Van de Graaff (VDG) at the Air Force Research Laboratory (AFRL) at Wright-Patterson AFB produces a transient electric field and an oscillating direct current via discharge pulses. The first measured direct current oscillation of the VDG has a rise time of $15 \times 10^{-9} \pm 5 \times 10^{-9} (s)$. This is within the validation range compared to the military standard (MIL STD) for the free-field EMP environment that has a rise time of $2.5 \times 10^{-9} (s)$, as shown in Figure 1. However, the fall time of the pulse produced from the VDG is three times too short for validation testing. The VDG's first direct current oscillation was measured to be a sine wave with a fall time of $15 \times 10^{-9} \pm 5 \times 10^{-9} (s)$ while the MIL-STD-464 is an overdamped pulse with a fall time of $55 \times 10^{-9} (s)$.

The VDG was found to produce an underdamped oscillating direct current pulse that is damped with time. Therefore, the purpose of this thesis study was to determine if the circuit resistance could be overdamped or critically damped; then the current pulse would more closely model the MIL-STD-464 free-field EMP environment.

This research focused on measuring and evaluating the direct drive current (current flowing through the strike plate) that is produced from the VDG. It was assumed that the time dependence of the current must be the same as with the free form electric field.

The goal of this research was to analyze the current pulse, and to explore whether the system variables of spark gap resistance (which is spark gap length dependent), equipment shielding, impedance matching, air breakdown saturation point, and circuit series resistance could be changed or modified so as to change the underdamped oscillatory current pulse into that of an overdamped system, thus meeting the free-field MIL STD EMP environment parameters. This research relied on the establishment of a reliable and repeatable method for obtaining current pulses from the VDG, to produce a current that has the potential to be used for direct current EMP survivability testing.

1.3 Overview and General Approach

The research of Dr. Charlesworth and Staniforth has modeled the VDG as an RLC (resistor, inductor and capacitor) circuit, which has solutions analogous to the equations for a damped harmonic oscillator [5]. Since the current flowing through the spark gap, cannot be measured directly, this research was oriented on the direct current at the strike plate. The oscillating current, which resulted from an electrostatic discharge of the VDG, was examined in order to determine if the oscillations could be depressed via overdamping of the RLC circuit. The purpose of which was to establish the degree to which the circuit could be used for direct current EMP survivability testing.

To measure the direct current from the strike plate, a current viewing resistor (CVR) was attached to the support cable of the strike plate. The CVR linearly converted the current to a voltage signal which was measured on an oscilloscope. This time dependence voltage pulse was analyzed for current amplitude and frequency. The

general layout of the experiment is shown in Figure 2, in which was measured the voltage versus time. Current was then derived from a known value of the resistance of the CVR.

With the changing electric field that was generated by the VDG, magnetic fields as well as conduction currents were produced. Equations that are used in evaluating EMP are Ohm's Law (Equation (2)), and two of Maxwell's equations; Faraday's Law and Ampere's Law (Equations (3) and (4), respectively).

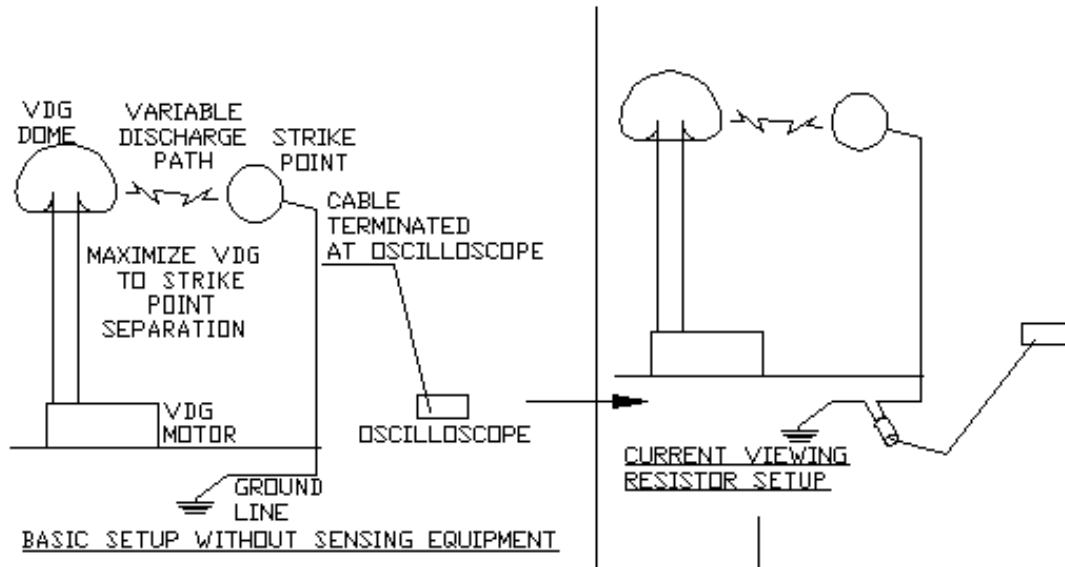


Figure 2. Experiment concept plan for direct current measurement [6].

$$V = IR \quad (2)$$

$$-\frac{\partial \vec{B}}{\partial t} = \nabla \times \vec{E} \quad (3)$$

$$\mu_0 \vec{J}_o + \epsilon_o \mu_0 \frac{\partial \vec{E}}{\partial t} = \nabla \times \vec{B} \quad (4)$$

Ohm's Law states that voltage (V), current (I) and resistance (R) are interdependent. Faraday's Law shows that changing magnetic fields (\vec{B}) are generated by electric fields (\vec{E}), and Ampere's Law says that conduction currents (\vec{J}_c) are generated by magnetic fields and/or changing electric fields.

For MIL-STD-464, the electromagnetic pulse fields, \vec{E} and \vec{B} , are modeled as double exponential functions of time dependent fields from the product of a rise and a decay function, as shown in Equation (6) that are developed from Equation (5) [3].

$$\begin{aligned} B(t) &= (\text{rising function})(\text{decaying function}) \\ B(t) &= (1 - e^{-t/\tau})(B_o e^{-at/\tau}) = B_o (e^{-at/\tau} - e^{-(a+1)t/\tau}) = B_o (e^{-at/\tau} - e^{-bt/\tau}) \end{aligned} \quad (5)$$

In Equation (5), B_o , is the initial magnetic field (not the maximum); a is the discharging coefficient, b is the charging coefficient where $b = a+1$, and τ is the time constant of the charging source function. Since the magnetic and electric fields are related through the constant, c (the speed of light), the free-field MIL-STD EMP generated electric field is shown in Equation (6).

$$E(t) = cB_o (e^{-at/\tau} - e^{-bt/\tau}) = E_o (e^{-at/\tau} - e^{-bt/\tau}) \quad (6)$$

Using Ohm's law and a known resistance for the CVR, the current is determined through scaling the measured voltage, as shown in Equation (7).

$$I(t) = I_o (e^{-at/\tau} - e^{-bt/\tau}) \quad (7)$$

CHAPTER 2

THEORY AND MODELING

2.1 Overview of Van de Graaff Operations

The Van de Graaff (VDG) is a large capacitor with an air-filled discharge gap. The VDG transmits a current in a spark channel, following voltage breakdown of air between the high voltage terminal (the VDG dome) and the strike plate. This is shown in Figure 3. The VDG works on the principles of manipulating static electricity through the triboelectric series.

The property known as static charge is generated by an accumulation of mobile charged particles. Typically, matter is neutrally charged, meaning that the number of electrons and protons are the same. If an atom has more electrons than protons, it is negatively charged. If it has more protons than electrons, it is positively charged.

How strongly an atom holds on to its electrons determines its place in the triboelectric series. If a material is more likely to give up electrons when in contact with another material, it is more positive in the triboelectric series. If a material is more likely to capture electrons when in contact with another material, it is more negative in the triboelectric series.

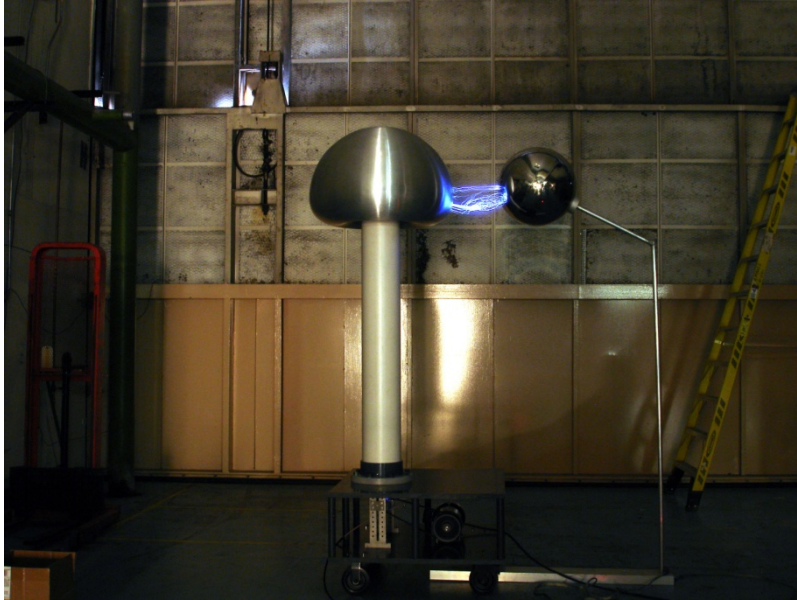


Figure 3. AFRL's Van de Graaff at Wright-Patterson, showing discharge to the strike plate.

The triboelectric series for common materials found in and around a VDG is given [7]; positive triboelectric materials in the series are at the top, and negative ones are at the bottom.

- Air (*Very positive - Gives up electrons*)
- Human hands (usually too moist, though)
- Human hair
- Nylon
- Aluminum (VDG bottom roller and dome head)
- Steel (*Neutral*)
- PVC (VDG structure)
- Polyurethane (VDG drive belt)
- Polytetrafluoroethylene (VDG top roller)
- Teflon (*Very negative - Captures electrons*)

The relative position of substances in the triboelectric series indicates how they will act when brought into contact. For example, polyurethane (VDG belt) brought next to aluminum (VDG bottom roller) causes a charge separation because they are separated

in the triboelectric series; the bottom roller gives up electrons and becomes positively charged while the belt captures electrons and becomes negatively charged, as shown in Figure 4. Since the belt surface area is larger than the roller surface area, the surface charge density will be greater on the roller than on the belt. The top roller made of polytetrafluoroethylene has a charge transfer exactly opposite from the bottom roller.

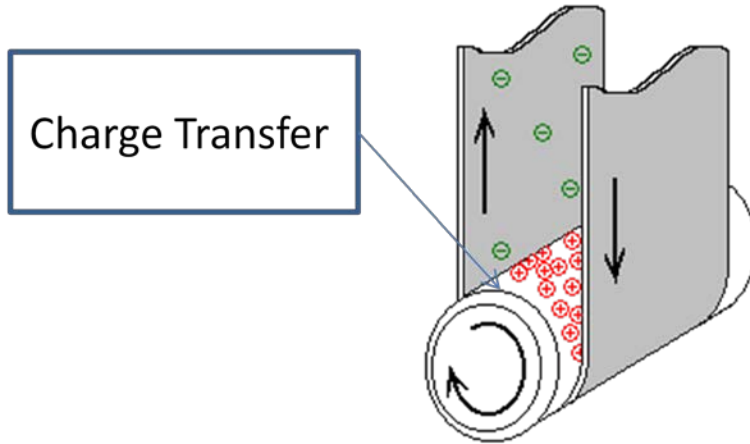


Figure 4. A charge transfer takes place from the roller to the belt. Adapted from [8].

The VDG system is a charge pump that turns the dome head into a charged capacitor. The VDG, as shown in Figure 3 is made up of a conveyor belt, made of polyurethane, and a pair of rollers (polytetrafluoroethylene, the top roller, and aluminum, the bottom roller) housed inside a structurally supported column made of PVC piping. A metal comb, not visible in Figure 3, is placed adjacent to each roller, as shown in Figure 5. The metal combs do not physically touch the roller or the belt so that the charge exchange is through a thin layer of air. A motor is used to drive the belt and move the charge.

In the AFRL VDG, the lower comb is attached to a 20 kV high voltage source, which can be used in either polarity. The high voltage source ionizes the air and either electrons or ions (depending upon the voltage polarity) are transferred onto the drive belt and carried to the capacitive dome. For all experiments in this thesis, the VDG was operated with the voltage source for primary charge transfer versus the triboelectric effect, in order to more rapidly charge the system. The VDG can be operated without the high voltage source, completely relying upon the triboelectric effect (See Appendix A).

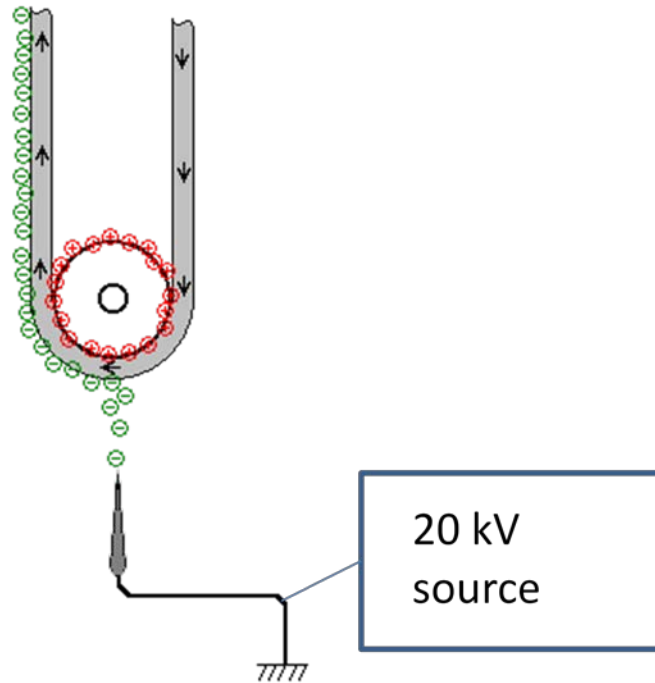


Figure 5. Diagram of high voltage source charging the VDG belt. Adapted from [8].

2.2 High Altitude Electromagnetic Pulse (HEMP)

The prompt gammas that escape a high altitude nuclear burst (well above the earth's atmosphere) are the driving force behind HEMP. The prompt gammas of 1.5×10^6 eV that travel into the earth's atmosphere interact with the atmosphere primarily through the Compton Effect. Compton electrons produce a flux of energetic electrons, which decelerate linearly due to collisions, and accelerate curvilinearly due to interaction with the earth's magnetic field [9]. These accelerating charges constitute a time-changing electric current, which generates a pulse of electromagnetic radiation according to Equations (3) and (4). These effects are described in Figure 6.

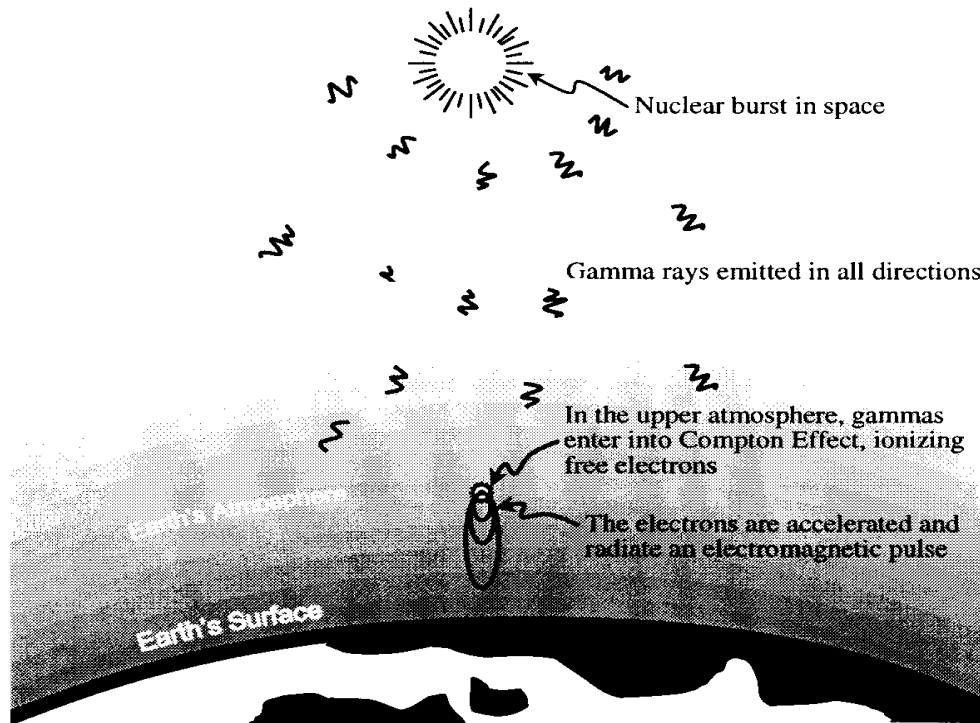


Figure 6. Diagram of situation that results in nuclear weapons generated High Altitude EMP (HEMP) [9].

The rise time of this current is a mirror of the rise time of the gamma rays, which in turn mirrors the weapon fission rise time. This fast rise time, faster than the rise time of a lightning strike, gives the EMP pulse a unique high frequency component [9]. The magnitude of an EMP voltage compared to a lightning strike, as well as electrostatic discharge is shown in Figure 7. The purely empirical expression for the EMP pulse as described by MIL STD 464 (see Equation (1)) is the difference between two exponentials. Bridgman states, “The double exponential form poorly represents the initial rise of the pulse and, as a result, misrepresents the high frequency content of the pulse” [9]. Nevertheless, the double exponential is the presently approved Military Standard pulse.

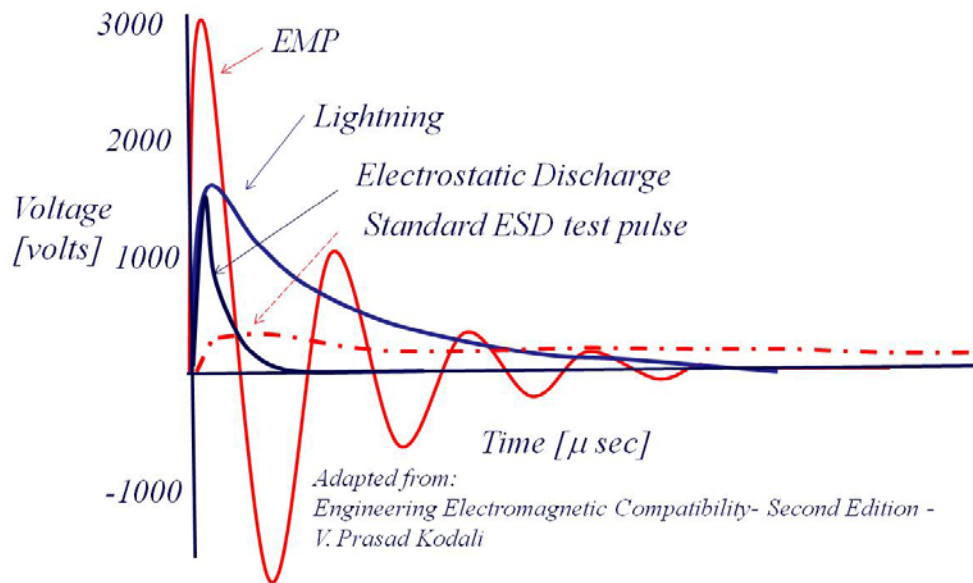


Figure 7. The magnitude of EMP, lighting and electrostatic discharge are compared [2].

2.3 Dielectric Breakdown of Air

Dielectric breakdown occurs when a charge buildup exceeds the electrical field limit or dielectric strength of a material. In the breakdown of air, the negatively charged electrons are pulled in one direction and the positively charged ions in the other. When air molecules become ionized in a very high electric field, air then changes from an insulator to a conductor.

Due to the very high electric field generated by the VDG, an oscillating current (known as a strike) will then occur between the dome head and the strike plate. Strikes occur because of the recombination of electrons in the air and ions on the strike plate. For example, lightning occurs when there is a buildup of charge on the clouds and in the air. This then produces the electric field between the clouds and the ground that exceeds the dielectric strength of air. Ionized air is a good conductor, and provides a path whereby charges can flow from clouds to ground, or in the VDG case, from the dome head to the strike plate.

This phenomenon, which is called dielectric breakdown, occurs in air at an electric field strength of about $E_{\max} = 3 \times 10^6$ V/m, at standard temperature and pressure. The exact value varies with the shape and size of the electrodes, and increases with the pressure of the air [7].

Personnel from AFRL provided the data on a single known point generated using the VDG. On Feb 4, 2010 at 11:12 a.m. the breakdown potential was measured as $V_{\text{BrkDwn}} = 2.75 \times 10^6$ V at an electrode separation distance, d , of 91 cm [10]. The temperature and relative humidity were 273.9 K and 73% [11].

The breakdown of air can be modeled as an underdamped RLC circuit that is controlled by the dielectric breakdown of air. A simulated breakdown of air and its curve fit is shown in Figure 8 [7]. The theoretical data shows a goodness of fit, or R^2 value, of 95% to a damped sine wave described by the equation: $I(t) = Ae^{-\alpha t} \sin(\omega t)$. Goodness of fit definitions are given in Appendix C.

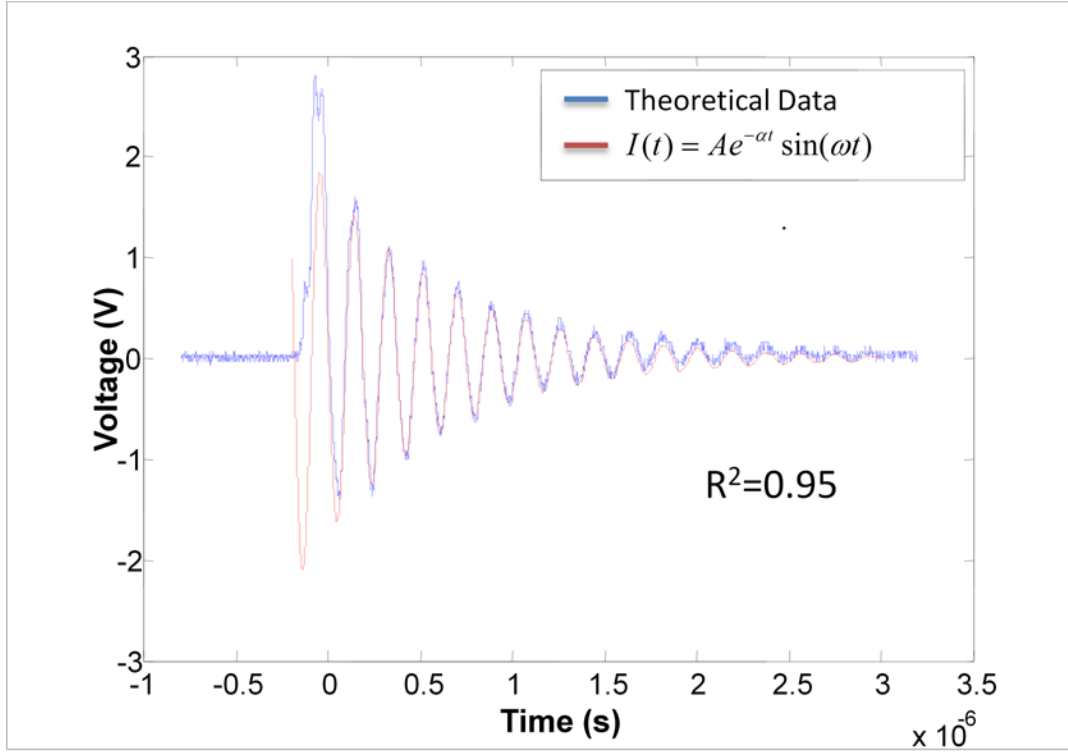


Figure 8. Voltage as a function of time illustrating that the VDG is an underdamped RLC circuit that is controlled by the dielectric breakdown of air. Adapted from [7].

2.4 RLC (Resistor, Inductor, and Capacitor) Circuits

Staniforth and Charlesworth's research showed that the VDG can be modeled after an RLC circuit [5][12]. The VDG RLC circuit is shown in Figure 9. Using

Kirchhoff's loop rule for an RLC circuit it was shown that the current was in the form of an oscillatory current pulse, and its amplitude is damped with time [12].

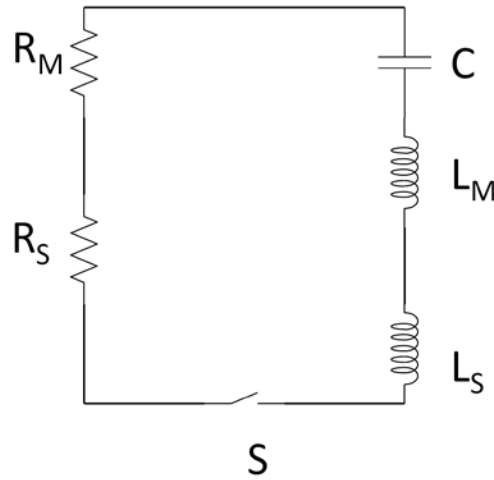


Figure 9. The VDG circuit can be simplified into a basic resistor, inductor, and capacitor (RLC) circuit.

For the VDG RLC circuit, the resistance, inductance and capacitance are given by R , L and C , respectively. The inductance and resistance for the spark discharge path are given by L_S and R_S , respectively. When air breakdown occurs, it is as though the switch “S” is closed and current flows through the circuit, with resistance of the dome, strike plate, and all other resistive and inductive parts of the VDG being represented by R_M and L_M . Because air has a resistance which depends on the current passing through the spark channel, the high frequency oscillations produced by the air breakdown are rapidly damped [13].

Simplifying this circuit was accomplished by adding the resistors and inductors in series, and then applying Kirchhoff's loop rule, which results in a differential equation as shown in Equation (8).

$$L \frac{dI}{dt} + IR + \frac{Q}{C} = 0 \quad (8)$$

Replacing I with dQ/dt in equation (8), a second-order linear differential equation with constant coefficients is obtained as shown in Equation (9).

$$L \frac{d^2Q}{dt^2} + R \frac{dQ}{dt} + \frac{1}{C} Q = 0 \quad (9)$$

Equations (8) and Equation (9) are analogous to the mass on a spring equation for a damped harmonic oscillator, as shown in Equation (10).

$$m \frac{d^2x}{dt^2} + b \frac{dx}{dt} + kx = 0 \quad (10)$$

In the oscillation of a mass on a spring, the damping constant b leads to a dissipation of energy. In an RLC circuit, the resistance R is analogous to the damping constant b of the spring and leads to a dissipation of energy.

If the resistance is small, the current oscillates with angular frequency that is very nearly equal to $\omega_0 = 1/\sqrt{LC}$. This frequency is called the natural frequency or resonance frequency of the circuit.

Equation (8) was shown qualitatively from energy considerations. Multiplying each term in equation (8) by the current, I , leads to Equation (11).

$$LI \frac{dI}{dt} + I^2 R + I \frac{Q}{C} = 0 \quad (11)$$

The magnetic energy in the inductor is given by $U_m = \frac{1}{2} LI^2 + C$. The derivative of the

magnetic energy leads to Equation (12).

$$\frac{d(\frac{1}{2}LI^2)}{dt} = LI \frac{dI}{dt} \quad (12)$$

Therefore, $LI \, dI/dt$, the first term in Equation (11), is the time rate of magnetic energy stored in the circuit. If $LI \, dI/dt$ is positive, it equals the rate at which electrical potential energy is transformed into magnetic energy. If $LI \, dI/dt$ is negative, it equals the rate at which magnetic energy is transformed back into electrical potential energy. Note that whether $LI \, dI/dt$ is positive or negative depends on whether I and dI/dt have the same sign or different signs. The second term in equation (11) is $I^2 R$, the rate at which electrical potential energy is dissipated in the resistor. This term is never negative.

The electric energy stored in the capacitor is shown in Equation (13).

$$U_e = \frac{1}{2}QV_c = \frac{1}{2} \frac{Q^2}{C} \quad (13)$$

The derivative of Equation (13) results in Equation (14).

$$\frac{d(\frac{1}{2} \frac{Q^2}{C})}{dt} = \frac{Q}{C} \frac{dQ}{dt} = I \frac{Q}{C} \quad (14)$$

IQ/C is the third term in Equation (11), and represents the rate of change of electric energy stored in the capacitor, which may be positive or negative. For the RLC circuit the sum of the electric and magnetic energies is not constant because energy is

continually dissipated in the resistor, thereby damping the oscillations. The solutions to the second order linear differential equation are shown in Appendix A.

2.4.1 Modeled RLC Circuits

MIL-STD-464 requires a single electromagnetic pulse for testing, while the VDG produces an oscillating sinusoidal current pulse. To better simulate the required pulse for MIL-STD-464, the RLC circuit of the VDG needs to be over or critically damped. The RLC circuit is the primary model for most high voltage and pulsed power discharge circuits. To illustrate this point an example of a series RLC circuit, as described in Figure 9, will be taken from an underdamped circuit to an overdamped then critical damped system [14]. This RLC circuit becomes a completed circuit when the switch (air breakdown between the VDG dome and the strike plate occurs) is closed. For this simulation the total inductance of the circuit is 10^{-6} H, the total capacitance is 10^{-6} F, the initial voltage on the capacitor is 10 V and the total resistance is varied between 0.2, 20 and 2 Ω to show the difference between the under, over, and critically damped situations.

2.4.1.1 Underdamped RLC circuit when $R^2 < 4L/C$

The current with a known capacitance, inductance and resistance were graphed. Figure 10 shows graphs of the under, over and critically damped cases when the resistance is varied between 0.2, 20 and 2 Ω . The under damped case is shown when the resistance is an order of magnitude (10x) less than the value required for a critically damped circuit. In Figure 10 the upper graph shows the current with a 0.2 Ω resistor.

The circuit current reaches its peak value at $\sim t = \pi / 2\omega_0$. The solutions to the underdamped model case are shown in Table 1.

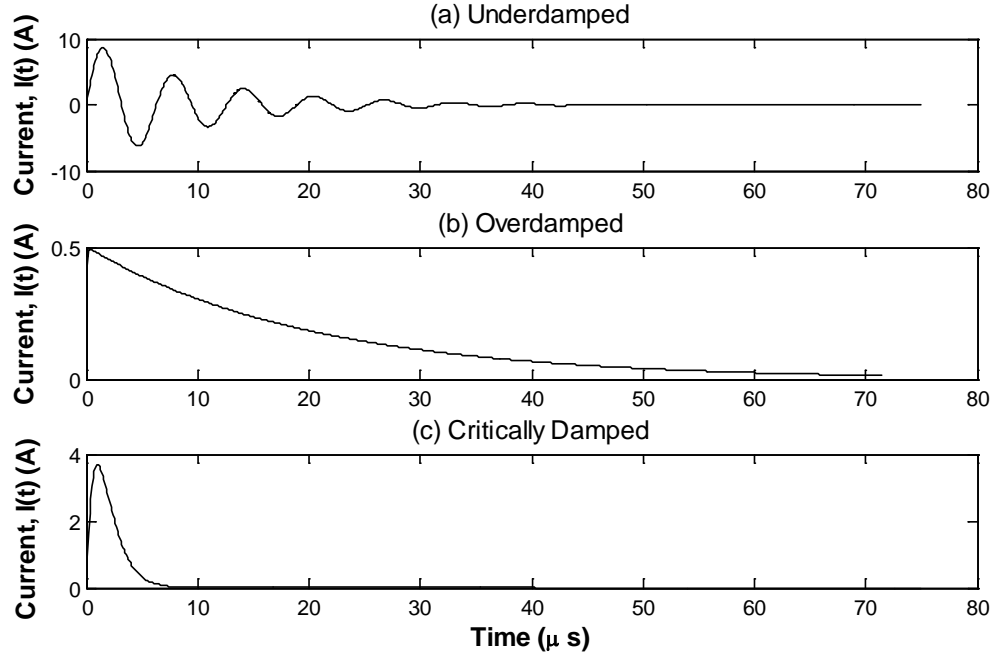


Figure 10. Current as a function of time is graphed for an under, over and critical damped RLC series circuit.

Table 1. Solutions to the underdamped second order linear differential equations for an RLC circuit [14].

| | | |
|---|--------------|---|
| $\omega_0 = \sqrt{\frac{1}{LC} - \left(\frac{R}{2L}\right)^2}$ | Omega | L is the circuit inductance (H) C is the circuit capacitance (F) R is the circuit resistance (Ω) |
| $i(t) = \left(\frac{V_0}{\omega_0 L}\right) e^{\left(\frac{-R}{2L}\right)t} \sin(\omega_0 t)$ | Current | V_0 is the initial voltage on the capacitance (V) |
| $I_{Peak} = \left(\frac{V_0}{\omega_0 L}\right) e^{\left(\frac{-R}{L\omega_0}\right)t}$ | Peak Current | Same as above |

2.4.1.2 Over damped RLC circuit when $R^2 > 4L/C$

The circuit schematic for the overdamped RLC circuit is shown in Figure 9. The resistance is an order of magnitude (10x) larger than required for a critically damped circuit with a resistance of 20 Ω .

The results of the overdamped circuit are shown in the middle graph of Figure 10. To drive this overdamped model the load resistor has a 20 Ω value. Once the switch closes the voltage on the load resistor rises to match the capacitor voltage and the current damps with time. The solutions to the underdamped circuit case are shown in Table 2.

Table 2. Solutions to the overdamped model case are shown [14].

| | | |
|--|---------|---|
| $\omega_0 = \sqrt{\left(\frac{R}{2L}\right)^2 - \frac{L}{LC}}$ | Omega | L is the circuit inductance (H) C is the circuit capacitance (F) R is the circuit resistance (Ω) |
| $i(t) = \left(\frac{V_0}{\omega_0 L}\right) e^{\left(\frac{-R}{2L}\right)t} \sinh(\omega_0 t)$ | Current | V_0 is the initial voltage on the capacitor (V) |

2.4.1.3 Critically Damped RLC circuits when $R^2 = 4L/C$

The circuit schematic for the critically damped model case is shown Figure 9. In this critical damped model, the resistance is exactly equal to the value required for a critically damped circuit, or $R^2 = 4L/C$ (with $R = 2 \Omega$). The results of the circuit model are shown in the bottom graph of Figure 10, and the solutions to the critically damped model case are shown in Table 3. In Figure 10 the circuit current reaches its peak value

at $t=2L/R$. This circuit is often desirable (if possible) with high voltage energy storage capacitors, since voltage reversals can frequently decrease the lifetime of the capacitor.

The modeled cases of the under, over and critically damped RLC circuit show that to meet MIL-STD-464 standard the circuit needs to be configured with R , L , and C so that the circuit is over or critically damped.

Table 3. Solutions to the critically damped model case.

| | | |
|--|--------------|--|
| $i(t) = \left(\frac{V_0 t}{L}\right)e^{\left(\frac{-R}{2L}\right)t}$ | Current | V_0 is the initial voltage on the capacitor (V) L is the circuit inductance (H) R is the circuit resistance (Ω) |
| $I_{Peak} = \frac{2V_0}{eR} \approx 0.736 \frac{V_0}{R}$ | Peak Current | Same as above |

2.4.2 Time dependence of the Spark Gap Resistance

In the simple RLC model of Section 2.4.1, R , L and C were constants. However, in the VDG the spark gap resistance (R_s) is time dependent. Staniforth and Charlesworth measured the spark gap resistance and showed that it depends on the current passing through the spark gap, which is time dependent for the VDG [12]. It was found that the variation of resistance for all gases through the spark gap can be approximated by using Equation (15).

$$R_s(t) = \frac{7.0 \times 10^{-4} \rho^{1/3} \ell}{\int_0^t i(t)^{2/3} dt} \quad (15)$$

In Equation (15), ρ is the gas density (kg/m^3) before breakdown, $i(t)$ is the time dependent spark channel current (A), and ℓ is the spark gap length (m). It was also

shown that the inductance (L) of the spark gap is independent of the gas pressure, damping increases with the terminal strike plate spacing, and $R_s(t)$ rapidly decreases with time [5]. The value of $R_s(t)$ is obtained at a particular time using Equation (15).

In the VDG analysis and research, the equipment to measure the spark gap current was not available, and manipulating the gas density in an open room was outside the scope. Therefore, the primary experiment to manipulate $R_s(t)$ was done by varying the spark gap length.

2.4.3 VDG Circuit Inductance and Capacitance

Energy storage via inductance occurs when current passes through a magnetic field. The inductance is related to the current and magnetic flux as $\Phi_m = LI$. In principle, the inductance of any coil or circuit can be calculated by assuming a current, I , and then calculating the magnetic field at every point on a surface bound by the coil or circuit, and then calculating the magnetic flux, and finally using $L = \Phi_m/I$. Since the current in the spark gap is time-dependent, the induction is also time-dependent.

Charlesworth and Staniforth measured the current flowing in the spark gap and found that the channel inductance is approximated by 1.4 nH/mm for both small (1.5 MV) and large (10 MV) VDGs [5][12]. Using this assumption and a spark gap distance of 6", the induction of the VDG was found to be 213×10^{-9} H.

The capacitance for the VDG was calculated to be 4.5×10^{-11} F [6], with the assumption that the VDG capacitance is calculated in three parts that are added together.

The top of the VDG dome is a capacitor that is made of a hollow aluminum hemisphere.

The capacitance of a sphere, C_{sphere} , is given in Equation (16).

$$C_{\text{sphere}} = 4\pi R_{\text{sphere}} \epsilon_o \epsilon_r \quad (16)$$

In Equation (16), R_{sphere} is the spherical radius of the VDG dome and ϵ_r is the dielectric constant. The hemisphere is set over the bottom half of the dome, which is a hollow, horizontally aluminum oriented toroid. An empirical equation for the capacitance of a toroid, C_{toroid} , in pF, is shown in Equation (17) [15].

$$C_{\text{toroid}} = \epsilon_r (0.37 D_{\text{Major}} + 0.23 D_{\text{Minor}}) \quad (17)$$

Therefore, the total capacitance of the VDG dome was found using Equation (18).

$$C_{\text{dome}} = \frac{C_{\text{sphere}} + C_{\text{toroid}}}{2} \quad (18)$$

The final capacitance component is the air volume capacitance, $C_{\text{AirVolume}}$. The air volume is that of the space between the two electrodes. This component is a function of the spark gap distance and is also calculated by changing Equation (16) to read:

$C_{\text{AirVolume}} = 4\pi R_{\text{air}} \epsilon_o \epsilon_r$. Therefore, C_{Total} is spark gap dependent. The capacitance of the VDG system is found by $C_{\text{Total}} = C_{\text{dome}} + C_{\text{AirVolume}}$.

2.5 Current Measurements via a Current Viewing Resistor (CVR)

An SDN-414-05 model, current viewing resistor (CVR) with a known resistance of $R=0.02651 \Omega$ was used to measure the time dependent current for electrostatic discharges from the VDG. This CVR model has a maximum band pass frequency of 2×10^9 Hz, a minimum rise time of 1.8×10^{-10} s, and a maximum energy of 2 joules [16], which was sufficient for all measurements in this thesis.

A sample energy calculation using typical values is shown in Equation (19) [6]. Using a maximum current of 450 (A) and a full width half maximum (FWHM) time of 2.91×10^{-7} s, the CVR is well within its design limits.

$$\begin{aligned}
 &\text{Energy (J), } E=i^2Rt=1.56 \times 10^{-3} \\
 &\text{Current (A), } i=450 \\
 &\text{Resistance (ohms), } R=0.02651 \\
 &\text{time (s) (FWHM), } t=2.91 \times 10^{-7}
 \end{aligned}
 \tag{19}$$

The use of the current to verify the time dependence of the spark gap electric field is problematic as the current through the CVR does not fully measure the spark gap current (and thus the electric field time dependence) for the spark gap. There are multiple measurement options for the current flow and energy storage in the circuit as noted in Chapter 3. To reduce these issues, impedance matching, shielding of cable and equipment, as well as placement of the CVR were analyzed.

2.6 Impedance Matching Measurements

The equipment used in this thesis is listed in Table 4. The cables, voltage source, oscilloscope, VDG and strike plate all have characteristic impedances. Pulse transmissions through coaxial cables are divided into two cases: 1) low-frequency, or slow pulses and 2) high-frequency, or fast pulses. The VDG generates electromagnetic pulses with frequency components into the MHz range, which are (by definition) fast pulses. A fast pulse has a rise time that is shorter than the cable transit time. For fast pulses, the characteristic impedance of the cable becomes important, because it describes the ability of the pulse to transit the cable unimpeded. This characteristic impedance depends on the dielectric material and diameter of the inner conductor and the outer shield of the cable; but is independent of the cable length, as shown in Figure 11. The properties of the coaxial cables used in this research are shown in Table 5.

Table 4. Equipment used in current measurements of the VDG.

| | |
|-------------------------------|---|
| Van de Graaff Generator (VDG) | Built at AFRL. The Arc of the Dome is ~ 7' above the floor. |
| Oscilloscope | Tektronix TDS 5104B |
| Current Viewing Resistor | T & M Research Products. SERIES SDN-414-0.025 |
| Power Supply (Generator) | No Manufacturer or Model Listed ID No.: C845588 S.N. N225035-01CJ090204 |
| Power Switch | General Electric Fuji AF-300 Mini Model NEMA 1XCID S.N.: 7BZ471A0008 |
| Cable | RG 58C/U with a Characteristic Impedance of 50Ω and Signal Propagation of $0.659 \times$ speed of light RG62A/U with a Characteristic Impedance of 93Ω and Signal Propagation of $0.840 \times$ speed of light |
| Connectors | BNC and commercial alligator clips |
| Shunt Terminators | 50 and 100Ω |
| Barometer | Nimbus Digital Barometer SN B6C8F2N01 |
| Signal Generator | Agilent 33220A – 20MHz Function |

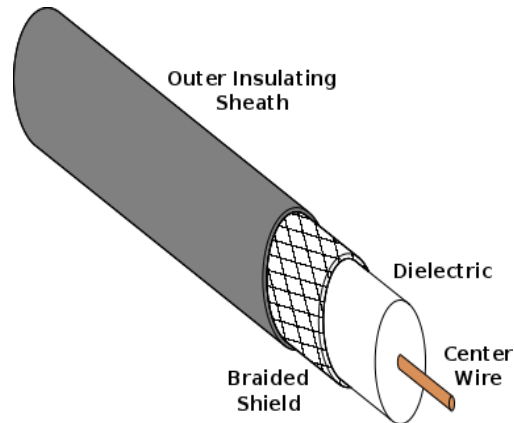


Figure 11. Construction of a standard coaxial cable. Adapted from [17].

Table 5. Properties of the coaxial cables used for all experiments [17].

| Cable Type | Insulating Material | Cable Diameter (cm) | Characteristic Impedance (Ω) | Signal Propagation (fraction of 3×10^8 m/s) | HV Rating (V) | Cable Capacitance (pF/m) | Signal Attenuation per Meter | |
|------------|---------------------|---------------------|---------------------------------------|--|---------------|--------------------------|------------------------------|-------|
| | | | | | | | MHz | dB |
| RG-58C/U | Polyethylene | 0.50 | 50 | 0.659 | 1900 | 100.1 | 100 | 0.174 |
| | | | | | | | 400 | 0.413 |
| RG-62/U | Polyethylene | 0.61 | 93 | 0.840 | 750 | 44.3 | 100 | 0.102 |
| | | | | | | | 400 | 0.207 |

Impedance is considered matched when the voltage source, V_S , equals the voltage load, V_L , as shown in the schematic of Figure 12. When impedance is matched, maximum power is transferred from source to load, and reflections along the transfer cable are minimized.

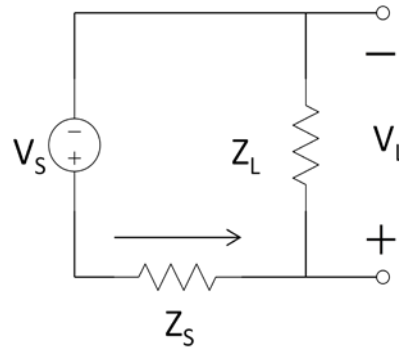


Figure 12. Circuit diagram for impedance matching. Adapted from [17].

In this circuit the impedance, $Z_T = Z_S + Z_L$, represents the opposition to the flow of energy from a source. For a constant current source (i.e. DC) the impedance is simply the circuit resistance, but for varying signals (i.e. AC) like those produced by the VDG, the impedance is a function of frequency. Impedance is represented as a complex value;

the real part represents the resistance, R , while the complex part represents the reactance, X , or the time dependent part. These relationships are shown in Equation (20) with j being the imaginary number.

$$\begin{aligned} Z &= R + jX \\ j &= \sqrt{-1} \end{aligned} \tag{20}$$

Both capacitive reactance X_C and inductive reactance X_L contribute to the total reactance, as shown in Equation (21); both are dependent on the frequency of the signal or system.

$$\begin{aligned} X &= X_C + X_L \\ X_C &= \frac{-1}{\omega C} = \frac{-1}{2\pi fC} \\ X_L &= \omega L = 2\pi fL \end{aligned} \tag{21}$$

If X is greater than zero, the reactance is said to be inductive. If X is less than zero, the reactance is said to be capacitive, and if X equals zero, then the impedance is all resistive. This happens when the magnitude of X_C equals the magnitude of X_L and happens at resonant frequency. At resonant frequency, maximum power is delivered from the current source to the current load.

2.7 Resonant Frequency

Resonance of a circuit involving capacitors and inductors occurs because the collapsing magnetic field of the inductor generates an electric current that charges the capacitor, and then the discharging capacitor provides an electric current that builds the

magnetic field in the inductor. This process is repeated continuously. An analogy is a mechanical pendulum.

Resonant frequency is reached when $\omega_o = 1/\sqrt{LC}$, as shown in Equation (22). At resonant frequency maximum power is obtained in the system, and therefore peak current is reached. Resonance is approached as reactance approaches zero and impedance is minimized. Experimentally, resonance is measured as voltage and current reach their peak values.

When the CVR was placed in line on the equipment experiments, the resonant frequency of the VDG system was experimentally found to be near 15 MHz. The equipment resonance experiment is described in Appendix B.

$$\begin{aligned} X_c &= X_L \\ 1/\omega C &= \omega L \rightarrow \omega^2 = 1/LC \rightarrow \omega_o = 1/\sqrt{LC} \end{aligned} \quad (22)$$

2.8 Skin Effect in metallic conductors

The skin effect is the tendency of an AC current to become distributed within a conductor such that the current density is largest near the surface of the conductor, and decreases toward the center. The electric current flows mainly at the skin of the conductor, between the outer surface and a distance called the skin depth. The skin effect causes the effective resistance of a conductor to increase at higher frequencies, where the skin depth is smaller, thus reducing the effective cross-section of the conductor. The skin effect is due to opposing eddy currents (I_w), induced by the changing magnetic field resulting from an AC current. At high frequencies, the skin depth becomes much smaller,

and the overall resistance of the conductor increases, which in turn decreases the current. This effect is shown in Figure 13 [17].

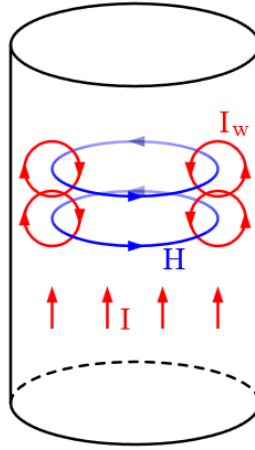


Figure 13. Skin depth is affected by eddy currents, I_w , that arise from a changing magnetic field. This effect reduces the current flow. Adapted from [17].

Coaxial cables in high-frequency electromagnetic fields are shielded by virtue of the skin effect. At frequencies at which the skin depth is comparable to or smaller than the braid strand thickness (e.g. around 100 kHz), the shielding is quite effective, but will become less so at higher frequencies. Under extreme conditions, it is sometimes necessary to surround the braid with a second shield to fully exclude the effects of very strong fields through which the cable must pass [17]. Doubly shielded coaxial cables are commercially available, in which a second braided shield is provided; however, another solution for difficult cases is to run a conventional cable inside tubing made of a solid conductor [17]. For this research the oscilloscope and the coaxial cables both need to be shielded to reduce electromagnetic interference (EMI). This was accomplished by shielding the coaxial cables with aluminum tape, as well as placing the oscilloscope on a

table (~ 3' from the floor) and 4' outside of the VDG room; also taking advantage of the field reduction with distance and shielding provided by the room walls.

2.9 Constructive and Destructive Reflections

Reflections in the coaxial cable are caused by abrupt changes in the electrical properties of the media through which the signal is propagated. This is commonly referred to as impedance mismatch. If the cable is connected to an electronic component, then the termination resistance is effectively just the input impedance of that component (i.e. oscilloscope). If the entire system is impedance matched then there will be no reflections and the load signal will not be diminished or enhanced due to constructive or destructive interference.

To minimize reflections, impedance matching is achieved by making the load impedance, Z_L , equal to the source impedance, Z_S . Ideally, the source and load impedances should be purely resistive. The transmission line (example RG-58C/U) connecting the source and load together must also have the same impedance: $Z_{load} = Z_{line} = Z_{source}$, where Z_{line} is the characteristic impedance of the transmission line. The transmission line characteristic impedance should also ideally be purely resistive. Cable makers try to get as close to this ideal as possible, and transmission lines are often assumed to have purely resistive characteristic impedances. This technique is known as reflection-less matching.

2.10 Effect of bridging and shunt terminators on circuit performance

Impedance bridging is defined when the load impedance, Z_L , is much larger than the source impedance, Z_S (i.e. $Z_S \ll Z_L$). Maximizing the load impedance serves to both minimize the current drawn by the load and to maximize the voltage signal across the load. The source impedance of the circuit is the combined internal resistance. Applying Kirchhoff's loop rule to Figure 12, Equation (23) resulted [17]. Equation (23) shows that if Z_S is low compared to Z_L , then $V_s \approx V_L$, and essentially all of the signal voltage is transmitted to the load (i.e. oscilloscope).

$$\begin{aligned} V_s &= iZ_s + iZ_L \\ V_L &= iZ_L \\ i &= \frac{V_L}{Z_L} \\ V_s &= V_L \left(\frac{Z_s + Z_L}{Z_L} \right) \\ V_L &= V_s \left(\frac{Z_L}{Z_s + Z_L} \right) \end{aligned} \tag{23}$$

To further reduce Z_S and enhance the bridging method, a resistor-to-ground (called a shunt terminator) was inserted parallel to the input of the oscilloscope so that the effective termination is the parallel combination of the source impedance and the shunt terminator resistance; effectively reducing the source impedance. As an example, a 100 Ω terminator added in parallel with an RG-62/U coaxial cable with a characteristic impedance of 93 Ω results in a total impedance of 48.18 Ω , as shown in Equation (24).

The bridging resistance of $10^6 \Omega$, and shunt terminator of 100Ω were used in all of the repeatable experiments on this thesis.

$$\frac{1}{Z_{parallel}} = \frac{1}{Z_s} + \frac{1}{Z_{terminator}} = \frac{Z_s * Z_t}{Z_s + Z_t} \quad (24)$$

2.11 Fast Fourier Transform (FFT) Algorithm for current pulses

To quantify the frequency components of each data for the VDG experiments, a Fast Fourier Transform (FFT) algorithm was used. A control experiment was completed to validate the FFT algorithm. A known signal source of 20 MHz and 5 V was transmitted through the VDG strike plate. This signal was then measured by the oscilloscope as shown in Figure 14. The FFT was used to analyze the frequency components. A single primary component of 20 ± 5 MHz was found, as shown in Figure 15. The error comes from the reflections of the impedance miss matches of the VDG system.

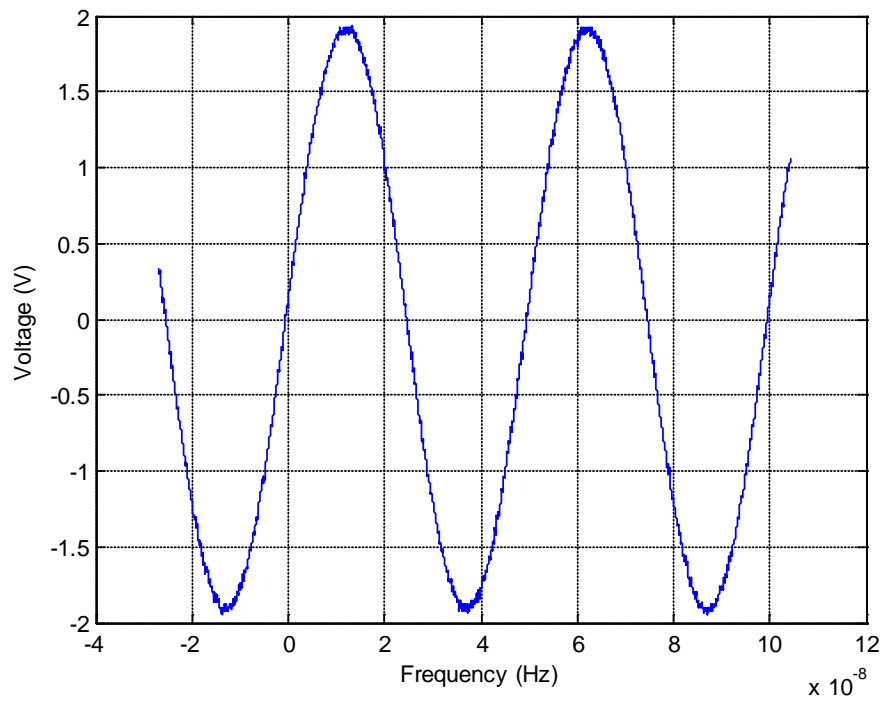


Figure 14. Known signal source of 20 MHz and 5 volts.

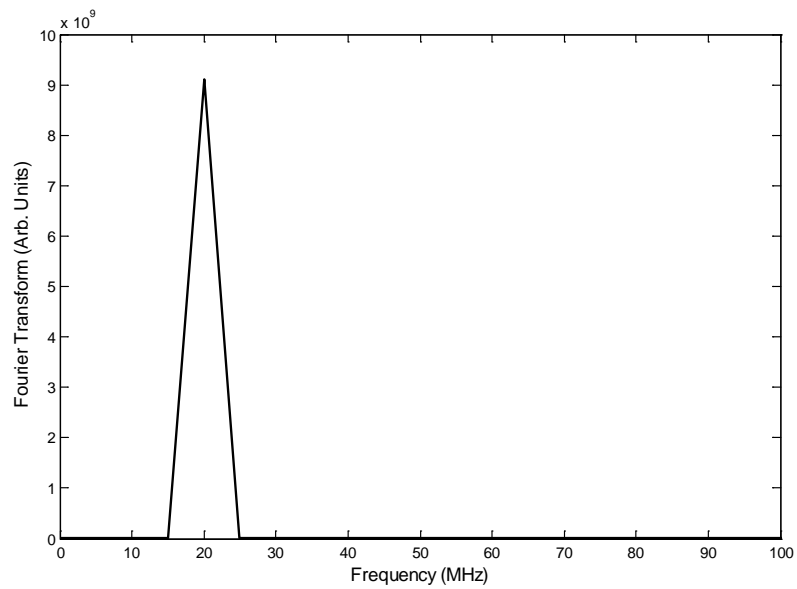


Figure 15. FFT for a 20 MHz 5 volt source.

2.12 VDG Measurements compared to current Models

2.12.1 Experimental comparison to the Damped Sine Wave model

All initial experimental current pulses from the VDG represented an underdamped circuit. To solve for the damping coefficient, Equation (25) was used [12].

$$\begin{aligned} i(t) &= Ae^{-\alpha_{12}t} \sin \omega t \\ \alpha_{12} &\approx \frac{\ln I_1 - \ln I_2}{t_2 - t_1} = \frac{\ln(I_1 / I_2)}{t_2 - t_1} \\ \omega &= 2\pi f \end{aligned} \tag{25}$$

The current magnitudes I_1 and I_2 were determined together with the associated times t_1 and t_2 , and the assumption was made that during the time interval $t_2 - t_1$, the damping coefficient α_{12} was constant so that the discharge current, i , could be expressed by $i(t)$.

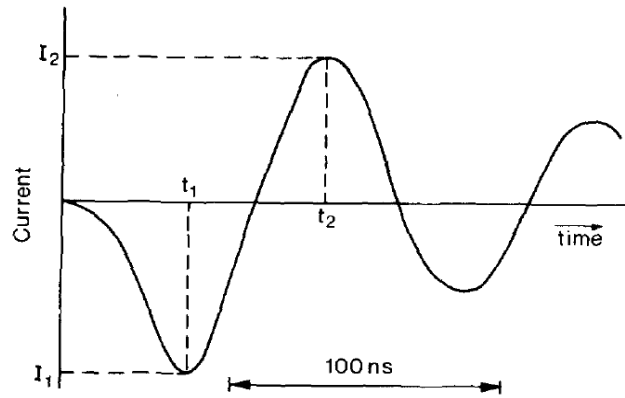


Figure 16. Typical discharge current pulse produced from a VDG (smoothed) [12].

Using an amplitude of 235 (A) and a frequency of 8.3 MHz, the damping coefficient was determined numerically using a least squares fitting routine, resulting in a

time dependent current of $I(t) = 235e^{5.0 \times 10^6 t} \sin[5.2 \times 10^7 t]$ which is plotted as a time dependent current pulse in Figure 17 (blue). For the data in Figure 17 a 3" spark gap was used. The first oscillation is closely modeled in rise and fall times, but the remainder of the oscillations do not fit the model well. This curve fit model is shown in Appendix C.

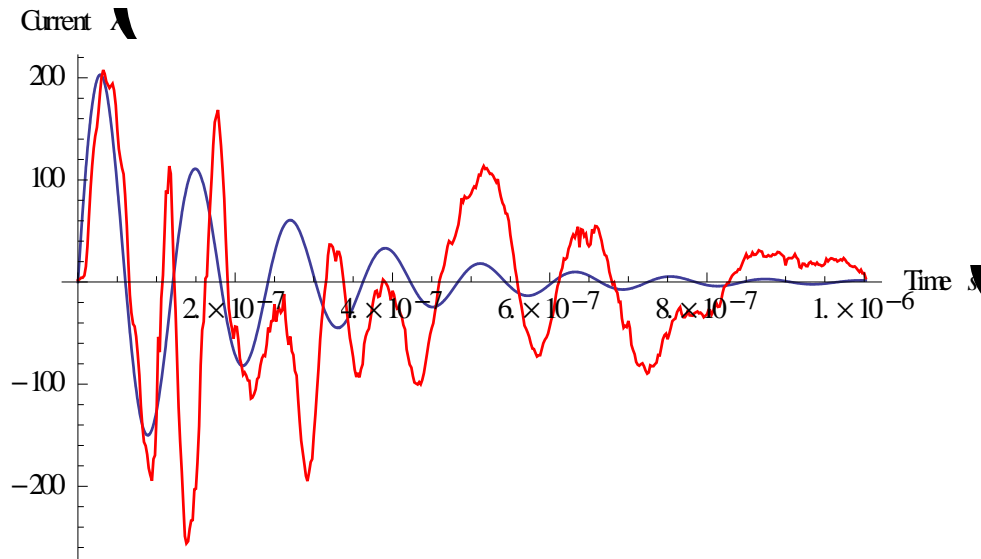


Figure 17. Raw data (red) overlaid on top of theoretical (blue) damped sine wave.

Comparing the theoretical damped sine wave (Figure 17) to the experimental data, a goodness of fit R^2 value -0.022 is obtained. A low R^2 value, or negative value, means it is a very poor curve fit. For a better curve fit only the first two oscillations were used and a R^2 value 0.54 was found, but when just the first oscillation was analyzed, then an R^2 value 0.92 was found.

This model was used on all of the repeatable data and showed that only the first oscillation had a R^2 value greater than 0.90. CVR connections, placement of RG-62 cable, transient electric field, time dependent spark gap resistance, humidity, and

temperature were all assumed to cause differences from the simple theoretical model. Therefore it was found that only an analysis of the first oscillation is repeatable and the modeling parameters of a single sine wave are useful.

2.12.2 Spark Gap Model

In an ideal RLC circuit R , L , and C are held constant but in the VDG R_s and L are time dependant and C is spark gap length dependent. Therefore, a model was developed to explore the effects of the time dependent current in the spark gap. The model solves the RLC circuit with a time dependent resistance based upon Charlesworth and Staniforth's equation for spark gap resistance, shown in Equation (15) [12], and the underdamped time dependent current, shown in Section 2.4.1.1 Table 1.

$$i(t) = \left(\frac{V_0}{\omega_0 L}\right) e^{\left(\frac{-R}{2L}\right)t} \sin(\omega_0 t)$$

$$\omega_0 = \sqrt{\frac{1}{LC} - \left(\frac{R}{2L}\right)^2}$$

$$R_s(t) = \frac{7.0 \times 10^{-4} \rho^{1/3} \ell}{\int_0^t i(t)^{2/3} dt}$$

The model methodology is shown in Table 6. R_s is the spark gap resistance, L is inductance, C is capacitance, ω_0 is angular frequency, and V_0 is initial voltage. The flow of the algorithm is from top left to top right, then down one row for the next iterative step. The model is shown in Appendix C.

At time zero, $\int_0^t i(t)^{2/3} dt$ was assumed to be 10^{-9} (A) so that a singularity would not exist when solving for the first step of R. For a spark gap maximum current of 2600 (A), as shown in Figure 25, the error introduced is small.

Table 6. Iterative algorithm to the time-dependent spark gap current.

Start here

→

Then ↓

| | $\int_0^t i(t)^{2/3} dt$ | R_s | w_o | $i(t)$ |
|-----------------------------------|---|--|---|---|
| At $t=0$ | 10^{-9} | $\frac{7 \times 10^{-4} \rho^{1/3} l}{\int_0^t i(t)^{2/3} dt}$ | $\sqrt{\frac{1}{LC} - \left(\frac{R}{2L}\right)^2}$ | $\frac{V_0}{\omega_0 L} e^{\frac{-R}{2L}t} \sin \omega_o t$ |
| $t=1 \times 10^{-11}$ (step 1) | $\int_0^t i(t)^{2/3} dt +$ $i(t)^{2/3} * dt$ | $\frac{7 \times 10^{-4} \rho^{1/3} l}{\int_0^t i(t)^{2/3} dt}$ | $\sqrt{\frac{1}{LC} - \left(\frac{R}{2L}\right)^2}$ | $\frac{V_0}{\omega_0 L} e^{\frac{-R}{2L}t} \sin \omega_o t$ |
| $t=2 \times 10^{-11}$ (step 2) | same | same | same | Same |
| ... | ... | ... | ... | ... |
| Until $t=t_{max}$ | ... | ... | ... | ... |

Using Charlesworth and Staniforth's known values for a 10 MV VDG, $L = 370\text{nH}$ and $C = 200\text{pF}$ [12], a spark gap of 3", and air density of 1.225 kg/m^3 , the time-dependent current was found as shown in Figure 18. To compare to known values, the spark gap resistance is also plotted, as shown in Figure 19; these values correspond well with the data in [12].

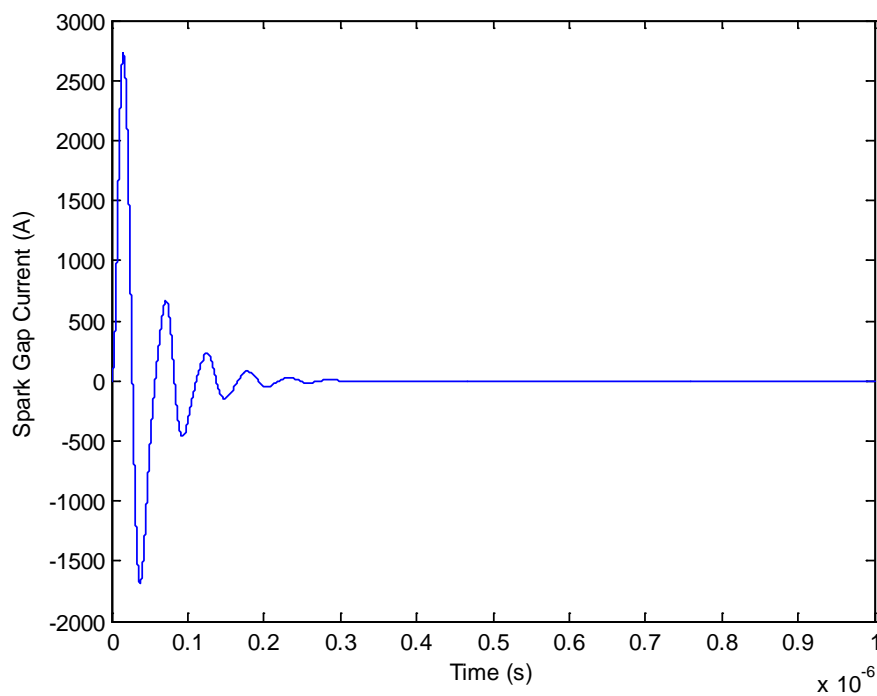


Figure 18. Spark gap time-dependent current is damped after 6 oscillations.

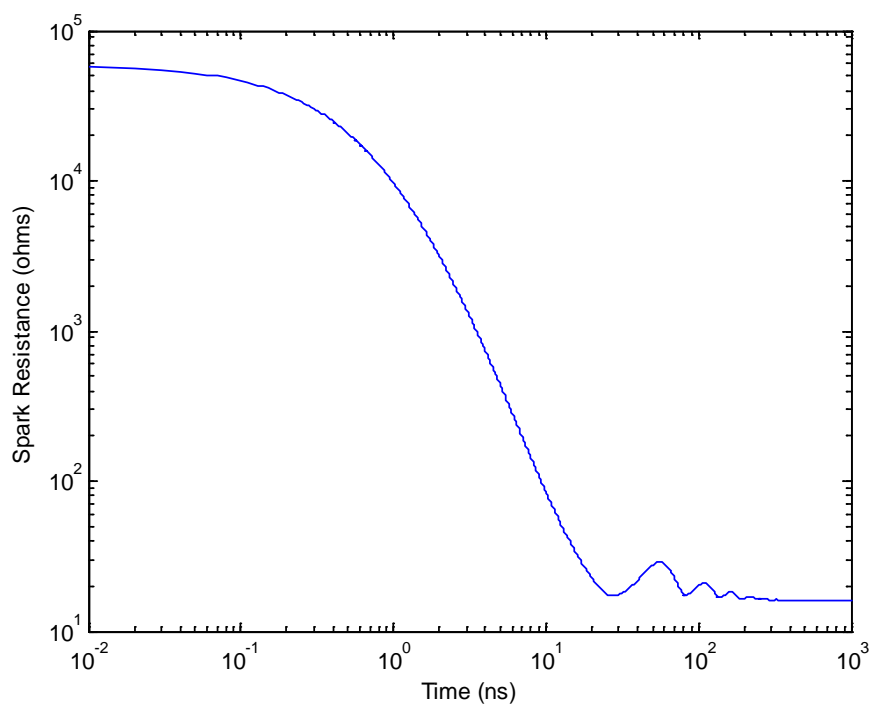


Figure 19. Spark gap time-dependent resistance decreases with time.

To compare the spark gap time-dependent current to experimental data, it had to be scaled to the measured current. The data for a spark gap of 3" is plotted against the scaled version of the modeled spark gap current, as shown in Figure 20. The modeled current is fully damped at $\sim 0.3 \times 10^{-6}(s)$, while the experimental data is damped after $10^{-6}(s)$.

Although an RLC circuit model provides initial insight into the expected current waveform, in this research the more physical results of adding a time dependent spark gap resistance were explored. The resultant model verifies that the time dependent current is oscillatory and damped with time. When comparing the modeled spark gap current to the direct current, even the first oscillation appears with reflective interference, as the model's first oscillation's primary frequency component is 15 MHz as compared to the experimental data of 8 MHz as determined from Fourier analysis.

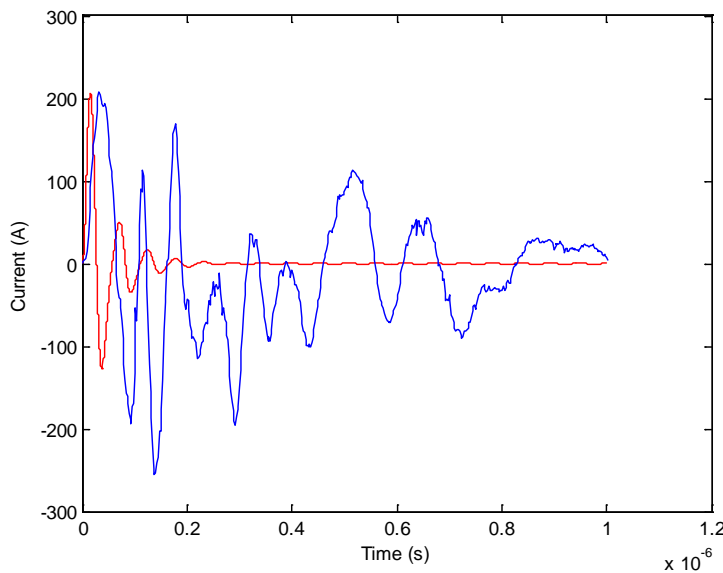


Figure 20. Scaled down spark gap current (red) compared to direct current (blue) for a 3" spark gap, and the CVR placed at position A on the support cable, as shown on Figure 22.

CHAPTER 3

VDG EXPERIMENTS

3.1 Equipment Confidence Experiments

3.1.1 Introduction

Equipment confidence experiments were conducted before subjecting the oscilloscope, coaxial cables (which were shielded with aluminum tape), and BNC connectors to the high currents generated from the VDG and the EMI (Electromagnetic Interference) from the transient electromagnetic pulse during an electrostatic discharge. All equipment confidence experiments were conducted with a signal source generator instead of the VDG, in order to gain confidence in the measuring equipment, and methodologies used.

A signal source generator was used to send a sinusoidal wave of fixed amplitude through the aluminum foil-shielded coaxial cables (RG-62/U and/or RG-58 C/U) to the strike plate, and then either into the CVR or directly into another shielded coaxial cable to the oscilloscope. The purpose was to verify that the wave was not distorted, and that the oscilloscope was reading the voltage signal correctly.

3.1.2 Response to Reflection-less (Impedance) Matching

Reflection-less matching was used as the baseline equipment confidence experiment. The signal source had an impedance of $50\ \Omega$, the RG-58C/U transmission cable had a characteristic impedance of $50\ \Omega$, and the oscilloscope was set to a $50\ \Omega$ termination. If impedance can be matched correctly then maximum power is

transmitted, and $V_S = V_L$. The voltage drops shown in Table 7 are from the skin effect at frequencies above 1 MHz, as well as characteristic cable impedance. This experiment demonstrated the skin effect theory. The signal source was connected directly to the oscilloscope through a coaxial cable; the data is shown in Table 7.

Table 7. Impedance matching for a coaxial cable experiment.

| Signal Source (50 Ω impedance) | | Oscilloscope (Terminated at 50 Ω) with RG-58C/U (50 Ω) cable of 15ft length | |
|--|---------|---|---------|
| Frequency | Voltage | Frequency | Voltage |
| 1 MHz | 1 V | 1 MHz | 1 V |
| 1 MHz | 5 V | 1 MHz | 5 V |
| 1 MHz | 10 V | 1 MHz | 10 V |
| 1 MHz | 5 V | 1 MHz | 5 V |
| 10 MHz | 5 V | 10 MHz | 4.92 V |
| 15 MHz | 5 V | 15 MHz | 4.92 V |
| 20 MHz | 5 V | 20 MHz | 4.88 V |

3.1.3 Response to Reflections (Impedance miss-matched)

The experiment was repeated, but with RG-62/U coaxial cables of different lengths. These cables have a characteristic impedance of 93 Ω , and would not be impedance-matched with either the signal source or the signal load of the oscilloscope since the source and load impedances were still 50 Ω . This had the effect of producing destructive interference and the oscilloscope indicated that the peak voltage was reduced compared to the reflection-less experiment; compare Table 7 to Table 8.

Table 8. Interference occurs when impedance is not matched using the RG-62 cables.

| Signal Source (50 Ω impedance) | | Oscilloscope (Terminated at 50 Ω) with RG-62 (93 Ω) cable of 3ft length | | Oscilloscope (Terminated at 50 Ω) with RG-62 (93 Ω) cable of 30ft length | |
|--|---------|--|---------|---|---------|
| Frequency | Voltage | Frequency | Voltage | Frequency | Voltage |
| 1 MHz | 1 V | 1 MHz | 0.98 mV | 1 MHz | 0.96 mV |
| 1 MHz | 5 V | 1 MHz | 5 V | 1 MHz | 4.88 V |
| 1 MHz | 10 V | 1 MHz | 9.98 V | 1 MHz | 9.80 V |
| 1 MHz | 5 V | 1 MHz | 5 V | 1 MHz | 4.88 V |
| 10 MHz | 5 V | 10 MHz | 4.98 V | 10 MHz | 4.32 V |
| 15 MHz | 5 V | 15 MHz | 4.94 V | 15 MHz | 4.84 V |
| 20 MHz | 5 V | 20 MHz | 4.88 V | 20 MHz | 4.10 V |

At high frequencies, the total reactance of Equation (21) was increased thereby decreasing V_L . The increase of the V_L for the 30' cable (i.e. 4.32 V up to 4.84 V) from the 10 MHz to 15 MHz is likely from resonance constructive interference as shown in Appendix B. The cable lengths also affected the measurements as cable capacitance is length dependent, as shown in Table 5. The added impedance caused by the increase of cable length decreases V_L from the 3 to the 30' cable length for all frequencies measured.

3.1.4 Response to the bridging and shunt terminator

The bridging method, having the load impedance Z_L much larger than the source impedance Z_S (i.e. ($Z_S \ll Z_L$)) for maximizing the voltage signal across the load was investigated. The oscilloscope was terminated at $10^6 \Omega$ and a shunt terminator of 50 Ω was added in parallel, the results are shown in Table 9. This method resulted in a clean

waveform and was used for all follow on experiments. For impedance matching a $50\ \Omega$ shunt terminator should be used on the RG-58 cable experiments and a $100\ \Omega$ shunt terminator for the RG-62 cable experiments; as these shunts match and closely match the respective characteristic cable impedances, as shown in Table 5.

Table 9. Impedance bridging and shunt terminator experimental data.

| Signal Source ($50\ \Omega$ impedance) Coaxial Cable RG-58C/U (15ft) | | Oscilloscope terminated at $10^6\ \Omega$ and a shunt terminator of $50\ \Omega$ | |
|---|---------|---|---------|
| Frequency | Voltage | Frequency | Voltage |
| 1 MHz | 1 V | 1 MHz | 1 V |
| 1 MHz | 5 V | 1 MHz | 5 V |
| 1 MHz | 10 V | 1 MHz | 10 V |
| 1 MHz | 5 V | 1 MHz | 5 V |
| 10 MHz | 5 V | 10 MHz | 5 V |
| 15 MHz | 5 V | 15 MHz | 5 V |
| 20 MHz | 5 V | 20 MHz | 5 V |

3.1.5 Response to CVR

To analyze the response of the CVR, two lengths of RG-62 coaxial cables were connected, as shown in Figure 21. The experimental data is shown in Table 10.

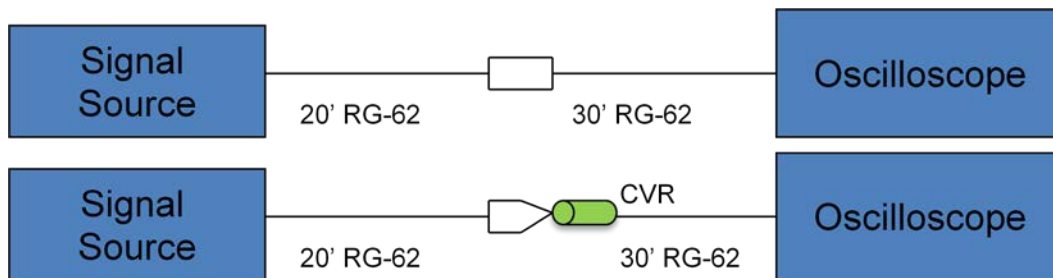


Figure 21. Two RG-62 cables and CVR equipment experimental setup.

Table 10. Two RG-62 cables and CVR experimental data.

| Signal Source (50 Ω impedance) | | Oscilloscope (Terminated at 50 Ω) with two RG-62 (93 Ω) cables of 50ft combined length | | Oscilloscope (Terminated at 50 Ω) with the two RG-62 (93 Ω) cables and the CVR placed in the middle | |
|--|---------|---|---------|--|---------|
| Frequency | Voltage | Frequency | Voltage | Frequency | Current |
| 1 MHz | 1 V | 1 MHz | 0.96 V | 0.93 MHz | 0.05 A |
| 1 MHz | 5 V | 1 MHz | 4.76V | 1.00 MHz | 0.18 A |
| 10 MHz | 5 V | 10 MHz | 4.36 V | 9.26 MHz | 0.08 A |
| 15 MHz | 5 V | 15 MHz | 4.37 V | 13.51 MHz | 0.09 A |
| 20 MHz | 5 V | 20 MHz | 4.84 V | 19.30 MHz | 0.10 A |

With a combined length of 50' for the two RG-62 cables the expected voltage drop, due to the characteristic impedance of the two cables, was measured on the oscilloscope. These cables have a characteristic impedance of 93 Ω , and would not be impedance matched with either the signal source or the signal load of 50 Ω . This produced destructive interference, reducing V_L . At high frequencies, the total reactance and the skin effect increase. Both of these effects cause a decrease in V_L . With the CVR in place, a resonant frequency (ω_0) of approximately 1 MHz was found, as a maximum current of 0.18 (A) was measured for the 1 MHz, 5 V source. This current was calculated using the 0.02651 Ω CVR. Resonance was approached at frequencies above 10 MHz as current began to increase again. When the CVR is placed in the system the measured current frequency decreases. This is likely do to circuit impedance differences between the coaxial cable and the CVR which resulted in reduced energy transfer and lower voltage.

3.1.6 Response to CVR Location

The purpose of these experiments was to find the best cable and connector attachment that would maximize the power throughput. In other words to find the best impedance matched circuit. The CVR was placed in numerous locations along the VDG and the power measured on the oscilloscope for a variety of sinusoidal waveforms. The two best matches were found when the CVR was placed in position A and position B, as shown in Figure 22. Position A was measured 12" from the base plate along the support cable. Position B was measured 63" from the base plate along the support cable, and Position C was measured 6" from the intersection of the support cable and the strike plate pole. These three CVR positions (position A, B and C) will be used to describe CVR location throughout this thesis. The response to the CVR in position A and position B will be described in this section.

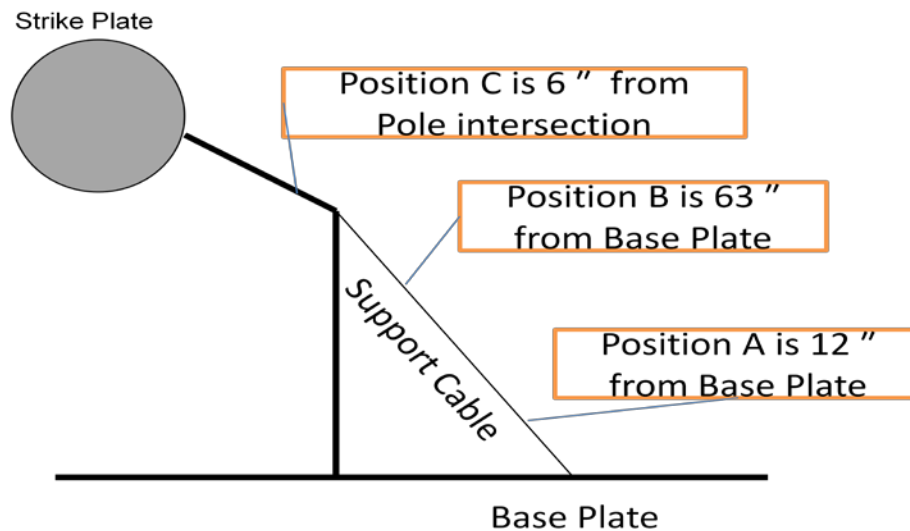


Figure 22. Position A, B and C for CVR locations.

These experiments were conducted with a constant frequency of 1 MHz, with peak voltages varying from 1-10 volts. This was then repeated, but this time the voltage was kept constant at 5 volts while varying the frequency from 1-20 MHz. The VDG circuit was set up by connecting the voltage source to the front of the strike plate using alligator clips and copper foil tape, as shown in Figure 23. The experiments were conducted with and without the CVR to determine CVR response. The data for the CVR placed on the back of the strike plate is found in Appendix B. The data for CVR in position B is shown in Table 11 and was compared to the data measured from position A shown in Table 12.

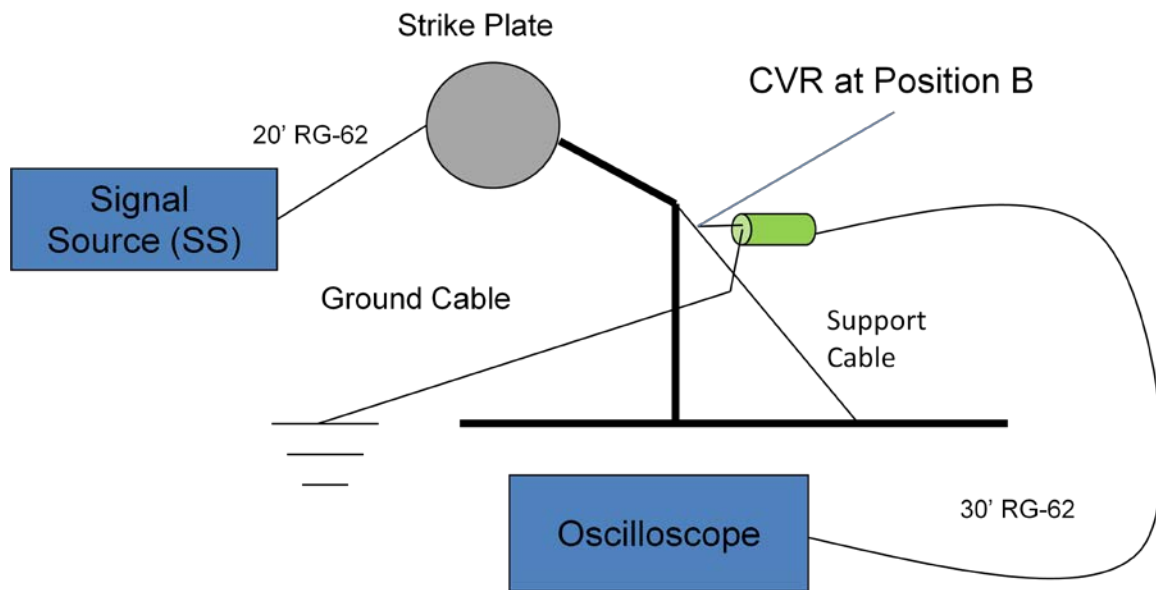


Figure 23. Experimental setup with CVR at position B.

Table 11. Experimental data with CVR placed at position B.

| Signal Source (50 Ω impedance) | | Without CVR (The oscilloscope was terminated at 50 Ω , RG-62 cables were used) | | With CVR (The oscilloscope was terminated at 50 Ω , RG-62 cables were used) | |
|--|---------|--|---------|---|---------|
| Frequency | Voltage | Frequency | Voltage | Frequency | Current |
| 1 MHz | 1 V | 1 MHz | 0.87 V | 0.89 MHz | 0.04 A |
| 1 MHz | 5 V | 1 MHz | 4.36 V | 1 MHz | 0.14 A |
| 1 MHz | 10 V | 1 MHz | 9.08 V | 1 MHz | 0.33 A |
| 1 MHz | 5 V | 1 MHz | 4.44 V | 1 MHz | 0.16 A |
| 10 MHz | 5 V | 10 MHz | 2.94 V | 10 MHz | 0.13 A |
| 15 MHz | 5 V | 15 MHz | 2.70 V | 15 MHz | 0.22 A |
| 20 MHz | 5 V | 20 MHz | 2.62 V | 19.80 MHz | 0.10 A |

The experiment was conducted again, this time with the CVR at position A, as shown in Figure 24. The data for position A is shown in Table 12.

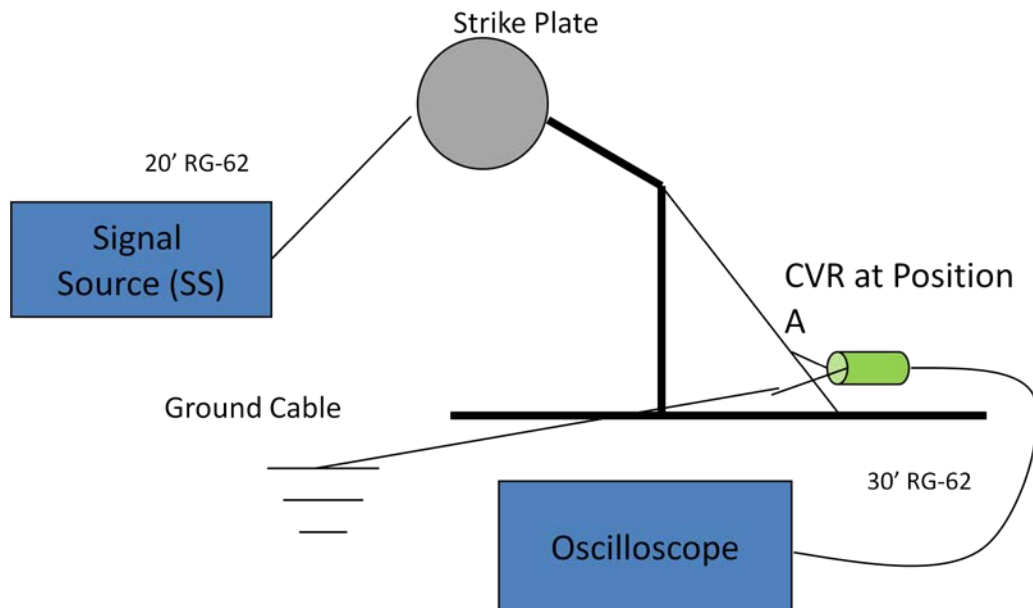


Figure 24. Experimental setup with CVR at position A.

The experiment was conducted to investigate the effect of the additional length of the support cable on the circuit response. Comparing Table 12 to Table 11, without the CVR, all but the 10 MHz frequency had a greater voltage drop than at position B. This was likely due to impedance mismatching, and added resistance from the extra support cable length. The increase of V_L found at 10 MHz for position A is likely due to the oscilloscope responding to a resonance frequency within the circuit.

When the CVR was placed at position A, the measured current was higher than when attached at position B for all frequencies except the 20 MHz range. This showed that there was a closer impedance match with the CVR at position A. This was also true for all other measured locations.

Table 12. Experimental data with CVR at position A. This is the best impedance match found.

| Signal Source (50 Ω impedance) | | Without CVR (Oscilloscope terminated at 50 Ω) | | With CVR (Oscilloscope terminated at 50 Ω) | | With CVR (Oscilloscope terminated at 10 ⁶ Ω & 100 Ω shunt terminator) | |
|--|---------|---|---------|--|---------|--|---------|
| Frequency | Voltage | Frequency | Voltage | Frequency | Current | Frequency | Voltage |
| 1 MHz | 1 V | 1 MHz | 0.86 V | 1 MHz | 0.05 A | 0.99 MHz | 0.12 A |
| 1 MHz | 5 V | 1 MHz | 4.34 V | 0.97 MHz | 0.17 A | 1 MHz | 0.24 A |
| 1 MHz | 10 V | 1 MHz | 8.84 V | 1 MHz | 0.33 A | 1 MHz | 0.41 A |
| 1 MHz | 5 V | 1 MHz | 4.36 V | 1 MHz | 0.17 A | 1 MHz | 0.26 A |
| 10 MHz | 5 V | 10 MHz | 3.24 V | 10 MHz | 0.26 A | 10 MHz | 0.64 A |
| 15 MHz | 5 V | 15 MHz | 1.28 V | 15 MHz | 0.53 A | 15 MHz | 0.75 A |
| 20 MHz | 5 V | 20 MHz | 1.05 V | 18.9 MHz | 0.08 A | 18.2 MHz | 0.16 A |

Because of the higher V_L measurements with the CVR placed at position A versus any other location, an additional experiment was conducted, but this time the oscilloscope was terminated at $10^6 \Omega$, and a shunt terminator of 100Ω was added in parallel, as shown in Table 12 as the last column. This significantly increased the measured current (greater than any other setup or CVR location). This experiment showed that positioning the CVR at position A and terminating the oscilloscope at $10^6 \Omega$, as well as adding a shunt termination of 100Ω in parallel, resulted in the best impedance match found, and was used for all follow on experiments.

3.1.7 Summary of Equipment Confidence Experiments

When the CVR was placed into the experiments, it was shown that the signal source had to be greater than 1 volt with a frequency greater than 100 kHz. If not, the oscilloscope was dominated by background noise. As the strikes from the VDG were in the thousands of volts and had frequency components in the MHz range, this was not a problem during the VDG pulse experiments. The signal source generator had a maximum output of 20 MHz and 10 volts; therefore, no equipment confidence experiments were conducted above these limits.

As described in the preceding sections, the characteristic impedance of the equipment and cables, as well as the resonant frequency, skin effect, reflections, and bridging/terminators, all affected the data. The use of the RG-62 shielded coaxial cables terminated into the oscilloscope at $10^6 \Omega$, and shunt terminator of 100Ω , transferred the greatest power to the oscilloscope with the least interference, as shown in Table 12, and was used throughout all of the remaining experiments. It was also determined that when

the CVR is placed at position A, as shown in Figure 22 there is a resonant frequency of 15 MHz, as shown in Appendix B, as the maximum power (e.g. voltage) was measured.

3.2 Response to VDG Equipment Setup

A schematic of the major equipment components and general VDG experiment is shown in Figure 25. The VDG was moved 1 to 18" away from the strike plate to find the results of spark gap distance. The oscilloscope was kept on a 3' high table placed 4' outside the VDG room to minimize EMI. The control station for the belt roller motor was placed inside the VDG room, and the 20kV high voltage source was supported off the ground with a wooden stool 3' away from the VDG. The 30' aluminum taped RG-62 coaxial cable was supported off the ground by two plastic columns, so as to minimize EMI and ground current coupling.

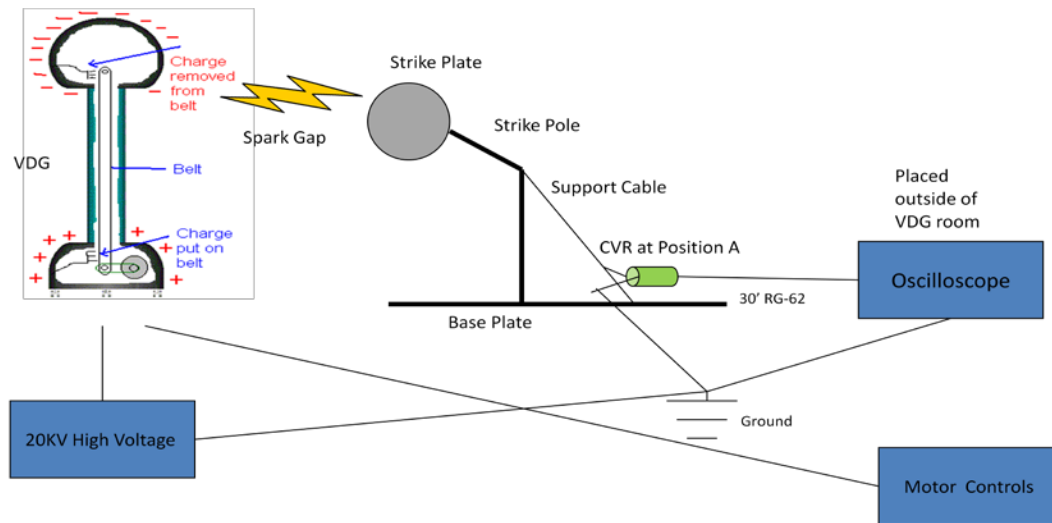


Figure 25. The Van de Graaff experimental setup used for all VDG experiments.

A 20 kV high voltage source was used to speed up the charging of the VDG capacitance, as described in Section 2.1. It was determined by experiment that the

current pulse amplitude and major frequency components of the wave were unaffected by the magnitude of the high voltage input. It did, however, increase the frequency of strike discharges between the VDG and strike plate. It was also found that the discharge would impact the strike plate, causing the strike plate to move in between strikes, which momentarily changed the spark gap distance. Through trial and error experiments, a minimum of 6 (s) was needed between strikes for the strike plate to fully return to its original location and stabilize the spark gap. Therefore, the high voltage source was kept as low as possible, so as to produce strikes between 7 and 8 (s).

It was also determined that the speed of the motor that turns the VDG belt did not affect the waveform. However, it also impacted the frequency of the discharges. To reduce the number of variables, the motor was kept at 30 RPM for all experiments and the high voltage was manipulated to control the time interval to a minimum of 7 (s) between strikes.

If the spark gap was too great a strike would not occur. The maximum spark gap was found to be between 9 and 18", depending upon environmental conditions (e.g. humidity, temperature and wind). It was also found that spark gaps greater than 9" gave very erratic current pulses (i.e. large amplitude, and variable frequency of oscillation) making the VDG unpredictable. It is likely (and was qualitatively observed) that for larger spark gaps, the current path and strike point would substantially change for a set of strikes. Wind travelling through the room (via poorly sealed windows or an open door) also reduced the frequency of strikes and the maximum spark gap. This is likely due to the wind removing ionized atoms, such as ozone, that would assist in initiating the strike. On days when the wind was not blowing the current pulses would stabilize after 20

strikes. Therefore, for each experiment, a set of conditioning strikes were measured until the current pulses were consistent. Then data would be collected.

With numerous trial and error experiments it was found that the connection of the CVR was critical for reliable and repeatable current pulses. It was found that a poor CVR connection could give momentary good results but then the current pulse would change. It was observed, at times, that a small spark gap resulted from poor CVR connections to the cable. Therefore, copper mesh clamps were used to better connect the CVR to the support cable, as shown in Figure 26. This resulted in a noticeable difference in the current pulse, in which fewer frequency components were observed, and measured by FFT. The primary difference was that the first oscillation became the maximum peak of the current pulse, after which the signal was fully damped.

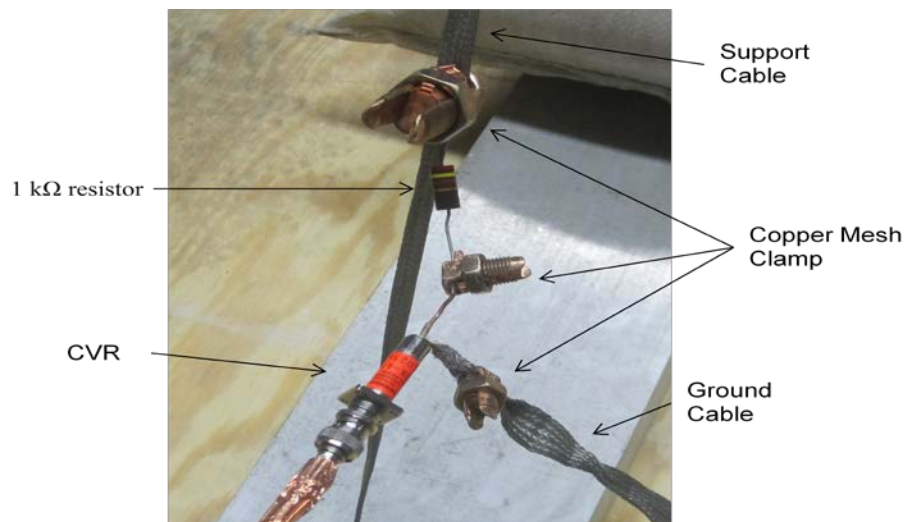


Figure 26. Copper mesh clamps were used to connect the CVR to the support cable and additional resistors.

It was also found by trial and error experiments that to have repeatable current pulses all equipment had to be isolated, as much as possible, from the concrete floor, as

shown in Figure 27. The next critical setup procedure was placement of the RG-62 shielded coaxial cable. The cable was positioned on support material and configured as shown in Figure 28. Once the VDG equipment was isolated from the concrete floor, the CVR had a solid connection, and the RG-62 cable was positioned so as to produce a maximum peak current in the first oscillation, reliable and repeatable current pulses were obtained. For the repeatable experiments, once a current pulse was measured in which the first oscillation was statistically (frequency and amplitude measured) stable, the RG-62 shielded cable was not moved for the rest of the experiments, as shown in Figure 28.

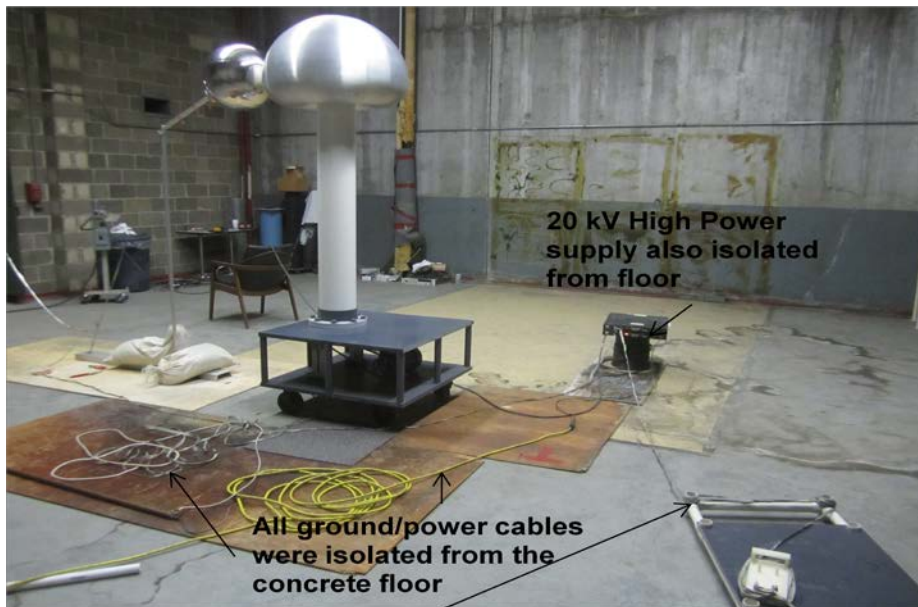


Figure 27. All VDG system equipment was isolated from the concrete floor.

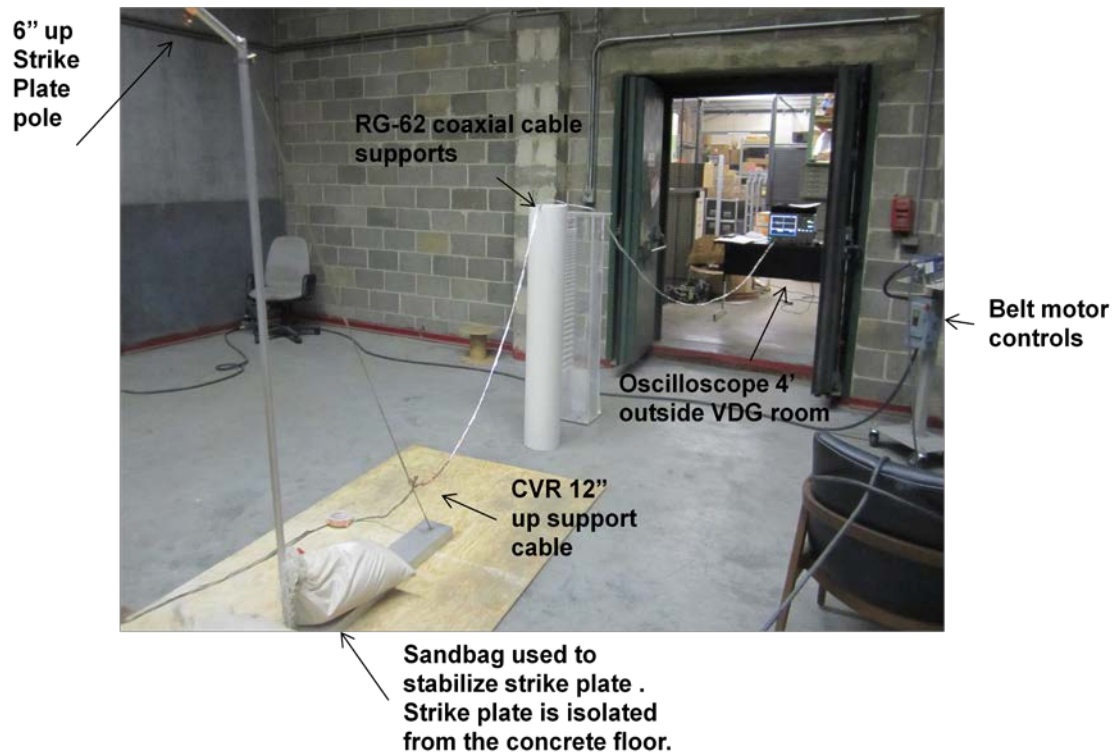


Figure 28. VDG setup with RG-62 shielded coaxial cables supported above the concrete floor.

To eliminate potential electrical noise from current sources within AFRL's Building B71, a new ground cable was installed. This new ground was connected directly to a grounding station outside of the building without any additional connections. With the new ground in place the repeatable setup, as described in this section were being followed and the results analyzed. However, the VDG transfer belt broke and this experiment was not completed. Initial data recorded following the establishment of the new ground was promising.

3.3 Impedance Response due to CVR Placement

In the equipment confidence experiments of Section 3.1 a signal source generator was used instead of the VDG. In these experiments the best waveforms were found with the CVR at position A (CVR placed 12" from the base plate along the support cable). The same types of experiments were conducted again, but this time with the VDG instead of the signal source generator, as shown in Figure 25. The results were the same as with the sinusoidal pulse (voltage source) measurements, validating the exercise. Some example data are shown in Figures 29 and 30.

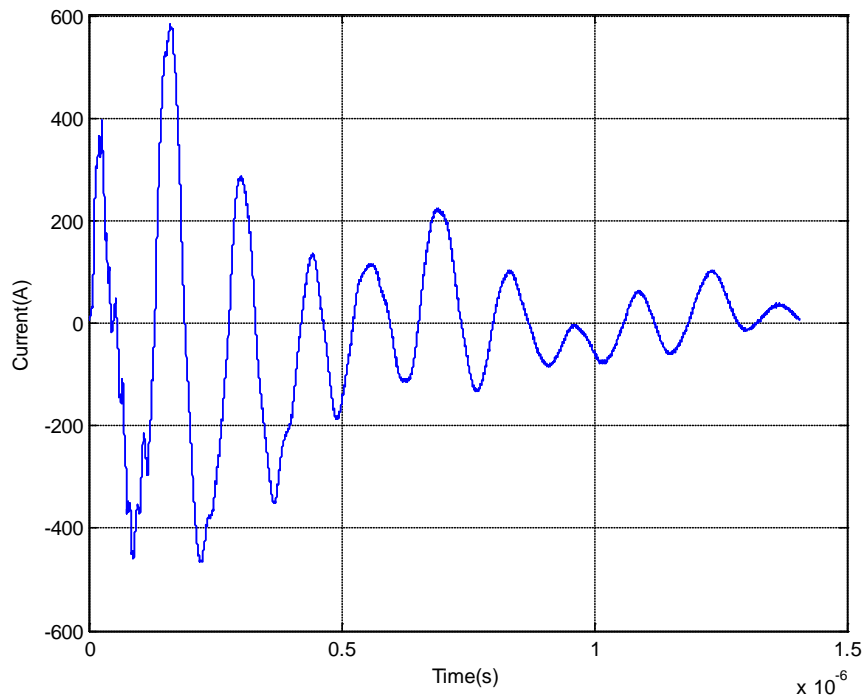


Figure 29. Current oscillations with CVR at position A.

Visual observation shows that position A is a cleaner waveform than position C. This is quantified by the FFT. The FFT for position A produced three primary frequency

components, while position C gave four primary frequency components. “Primary”, in this case, was defined as having at least a Fourier magnitude of 3×10^{10} , as shown in Figure 31.

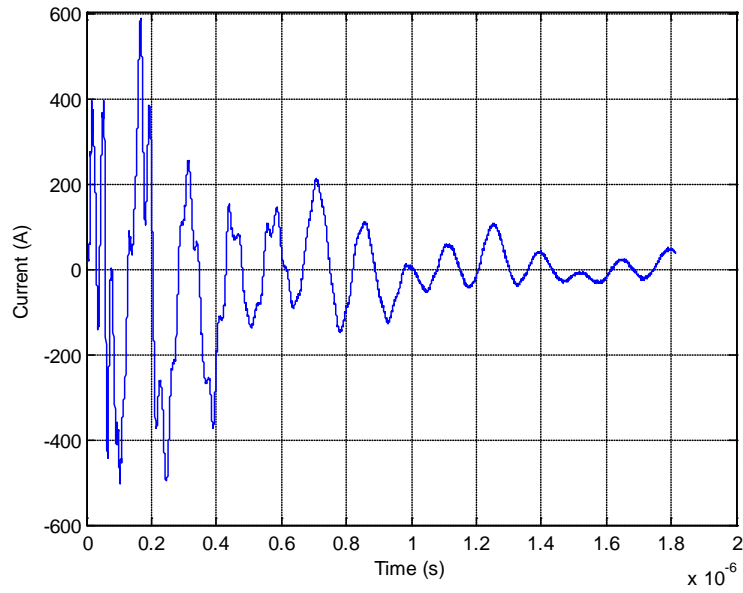


Figure 30. Current oscillations with CVR at position C.

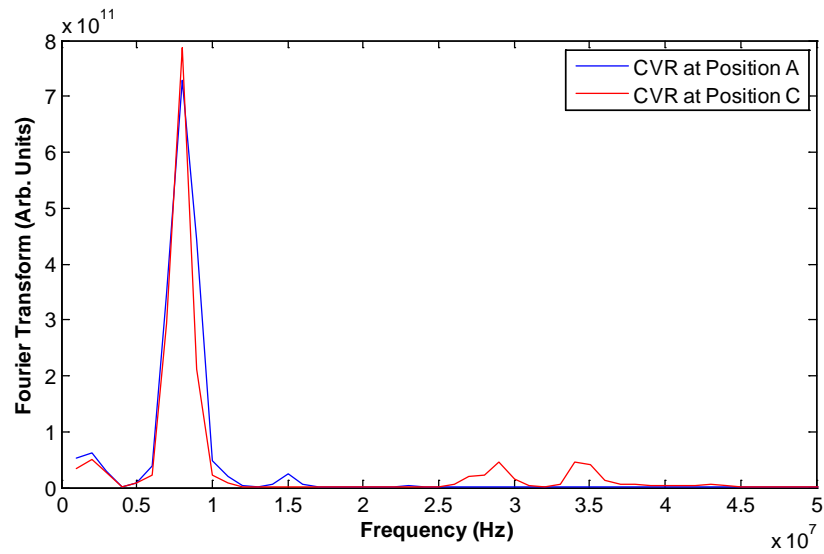


Figure 31. Plot of FFTs of full current pulses measured with the CVR at position A (blue) and position C (red).

Charlesworth and Staniforth's results confirm the data that was found in this thesis. They state a dominant frequency was excited in large [12] and small [5] VDGs (10 MV and 5 MV respectively) due to "...the inductance of the VDG resonating with the spark channel inductance. In some cases, a higher frequency, which is an electromagnetic mode supported by the whole machine, is also excited" [12]. The dominant frequency was spark gap and maximum potential dependent. A lower frequency of 31 ± 3.5 MHz and a higher frequency of 186 ± 17 MHz was found for the small 1.5 MV VDG [5]. An additional lower frequency of 10 to 13 MHz, and a higher frequency of 110 ± 20 MHz was measured for the shorter spark gaps and 230 ± 25 MHz for large spark gaps for the 10 MV VDG [12]. Both studies state "these higher end frequencies are probably associated with the high frequency electromagnetic modes which can be supported by the whole machine" [12] [5]. The VDGs used in these studies were enclosed and pressurized [5][12], but it was assumed that these methods are applicable for the present study.

The AFRL VDG was found to have three primary frequencies within the current pulse, compared to the two found for the Charlesworth and Staniforth studies. The same raw data that was used for the impedance matching and CVR location experiments, shown in Figure 29 and Figure 30 were used to analyze the frequency components via FFT. The FFT data, plotted in Figure 31 for both the CVR at position A and position C have a primary FFT of $8 \text{ MHz} \pm 1 \text{ MHz}$. They also both share a secondary dominant frequency of 2 MHz, but the tertiary dominant frequency components vary from 15 MHz for position A to 29 and 34 MHz for position C. The FFT algorithm confirms what the

raw data showed, which is, that attaching the CVR at position A results in a cleaner (fewer interference oscillations, likely due to better impedance matching), current pulse.

As another example, the FFT analysis was also applied to the current pulses measured with the CVR placed at position B. These results are shown in Figure 40. It is clear from this data that the primary frequency of 8 MHz is not as clearly defined as when the CVR was placed at position A or B.

Using both raw data and FFT analysis, it was proven that the cleanest signal (e.g. one with the fewest dominant frequency components) resulted with the CVR attached at position A. Positions A, B and C were the cleanest current pulses over all other locations. Therefore, position A was chosen for all follow on experiments.

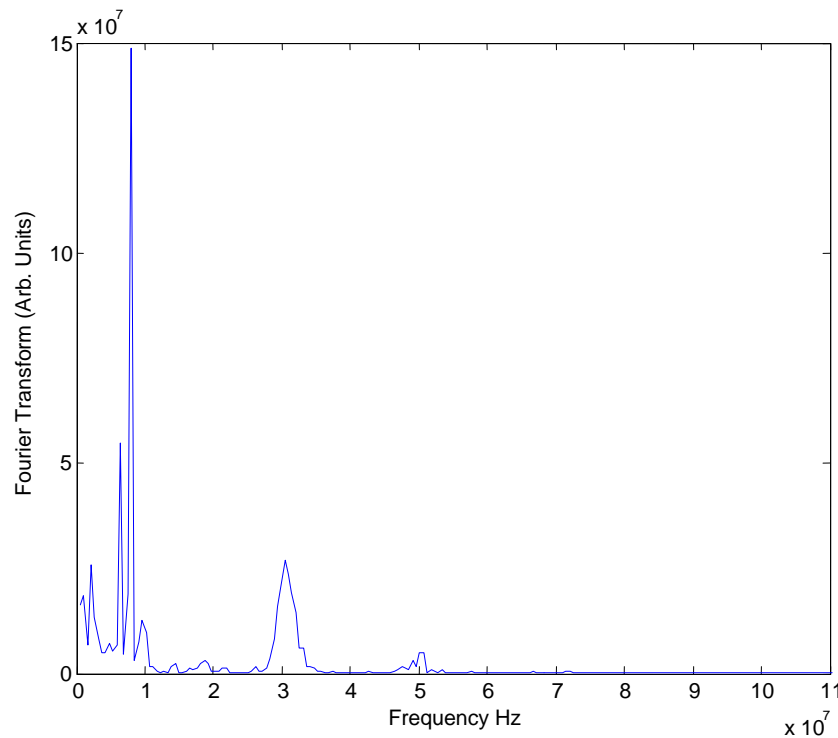


Figure 32. FFT of the current pulse measured with CVR at position B.

3.4 Response due to Spark Gap

Once the CVR location of position A was determined to produce the cleanest current pulse; which allowed repeatable strikes to take place, the effort was oriented on finding the least noisy measurement based upon the spark gap distance. The same method as in Section 3.3 was used. This method was to qualitatively assess the raw data waveform, followed by a FFT to determine the measurement with the least number of major oscillation frequencies. The time dependent current for the 3" spark gap, as shown in Figure 33, had fewer reflections and frequencies (on top of the primary current) than did the 7" spark gap, also shown in Figure 33. From all raw data qualitatively observed and recorded, the 3" spark gap produced the best impedance match over any other spark gap distance.

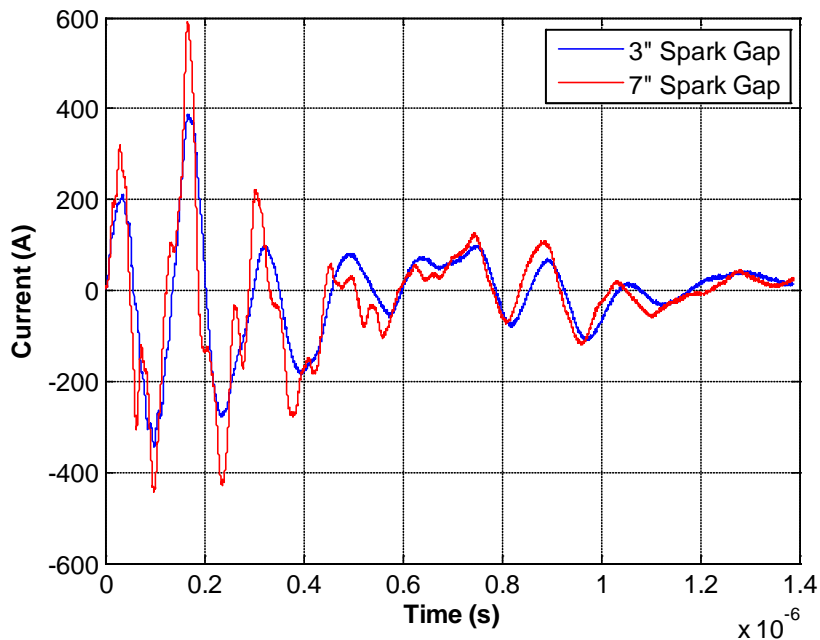


Figure 33. Current pulse for the 3" and 7" spark gaps.

Observation of the raw data showed that the 3" spark gap produced the cleanest current pulse, as shown in Figure 33. However, the FFT for the spark gaps ranging from 1 to 8" were all within ± 0.3 MHz for all three major frequencies. The primary frequency was measured at 7.5 MHz while the secondary frequency was measured at 2 MHz, and finally the tertiary frequency was found to be 14 MHz. These measurements were conducted with alligator clips for the CVR connection versus the copper mesh clamps. These results are ± 1.5 MHz different from those measured with mesh clamps, as shown in Tables 14-17. Nevertheless, the FFT results lead to the conclusion that the spark gaps of 3, 6, 7 and 8" should be used for the repeatable experiments.

3.5 Reliable and Repeatable Current Strikes

3.5.1 Environmental Set up

It was found that to achieve four days of repeatable current pulses the set up of the VDG system was critical and that Section 3.2 (VDG Equipment Set up) needs to be followed. Power projections through the measurement circuit were critical to the placement of the 30' RG-62 shielded coaxial cable. Previous experiments showed that placement of the cable could change the current amplitude by up to 117 (A). Positioning the cable, on the concrete floor, lead to the greatest decrease in the measured current. It was found that the RG-62 shielded coaxial cable must be supported off the ground, as ground current coupling takes place. It was also found that positioning the cable changed the amplitude and frequencies of the current pulses. Therefore, the cable was positioned to create an environment where the first current oscillation had the maximum current

amplitude. Once a suitable cable position was found it was kept in that position, as shown in Figure 28. The only time it was moved was when spark gap distance was changed.

3.5.2 Measurements with Repeatable First Oscillations

The four days of experiments had only slightly different humidity and temperature environments for the VDG room. These conditions are shown in Table 13. All experiments had the CVR placed at position A. Comparing current pulses for the 3" spark gap for experiment 1 to experiment 2 showed that the first oscillations of both data sets share the same measured frequency of $8.56 \text{ MHz} \pm 0.4 \text{ MHz}$ and approximate maximum current amplitudes of 200 (A); however, the amplitudes of the 2nd through 8th oscillations are distinctly different, as shown in Figure 34.

Table 13. Humidity and temperature environments for the repeatable experiments.

| Experiment | Humidity | Temperature (Fahrenheit) |
|------------|----------|--------------------------|
| 1 | 21% | 68 |
| 2 | 16-21% | 68 |
| 3 | 20% | 63 |
| 4 | 41% | 72 |

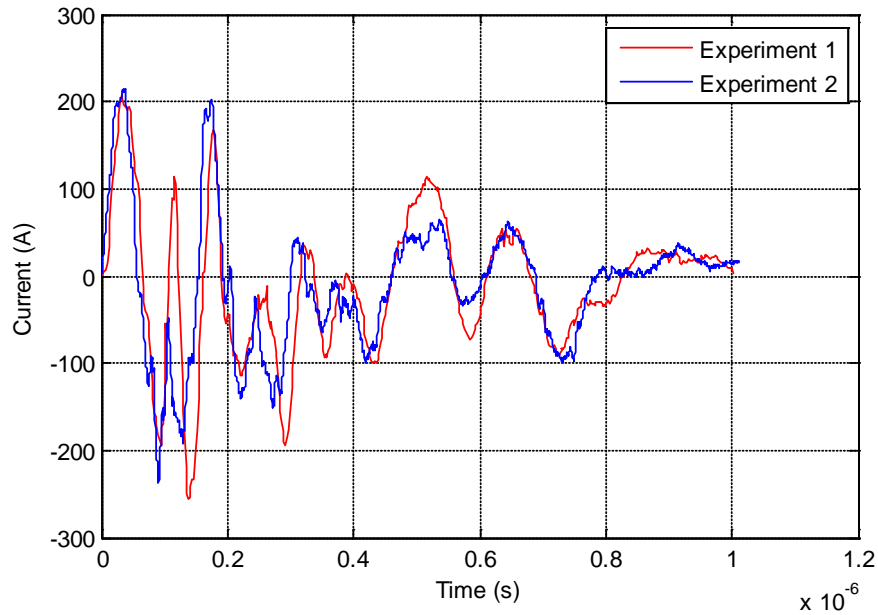


Figure 34. Raw data (current as a function of time) for 3" spark gap.

The data obtained for all repeatable experiments did not represent a damped sine wave. Nevertheless, the first oscillation rise and fall times, and maximum amplitude were repeatable. It was assumed that only the first oscillation is repeatable because the rise time of the first oscillation is completed before the transmission of the reflections have time to travel through the 30' coaxial cable.

The signal propagation through the RG-62 cable is $0.840c$, with c being the speed of light measured at 3×10^8 m/s [17]. Therefore, the transmission time of a reflection through a 30' coaxial cable is 3.63×10^{-8} (s). The rise time of the average first oscillation for the spark gap of 3" is $1.5 \times 10^{-8} \pm 0.3 \times 10^{-8}$ (s). This was the shortest rise time, while the 7" spark gap had the longest rise time of $1.0 \times 10^{-8} \pm 0.3 \times 10^{-8}$ (s). Therefore, it is assumed that the first oscillation is repeatable because reflected waves from the pulse cannot traverse the cable in time to interfere.

The FFT of the current pulse indicates the same dominant frequencies (3, 7 and 15 MHz \pm 2 MHz); however, the primary and secondary Fourier frequencies appear in a different order, as shown in Figure 35. The first oscillations of both experiments share the same measured frequency of 8.56 MHz \pm 0.4 MHz, as shown in Figure 34.

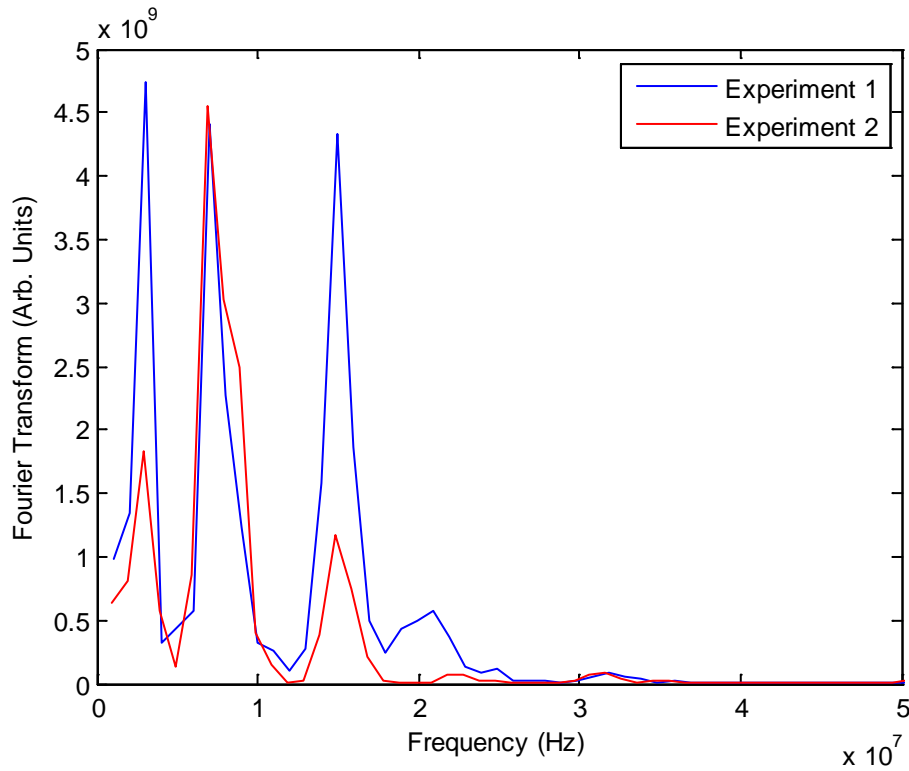


Figure 35. FFT for 3" spark gap for experiment 1 and 2.

It was found that over all 4 experiments the 3" spark gap had a measured average first oscillation frequency of 8.56 MHz \pm 0.4 MHz, while the 6" spark gap had a measured frequency of 13.95 MHz \pm 1.0 MHz, and 7" had a measured frequency of 15.78 MHz \pm 1.3 MHz, and finally the 8" spark gap had a measured frequency of 15.15 MHz \pm 1.1 MHz.

3.5.3 Model of the First Oscillation

The data from all four days of experiments are shown in Figure 36. It was found that only the first oscillation was statistically comparable and repeatable. Isolating the first oscillation from the full wave turns the general equation into a sinusoidal wave with a general model solution of: $I(t) = I_0 \sin[\omega t + \phi]$, where I_0 is the initial amplitude, ω is the angular frequency, and ϕ is the phase change.

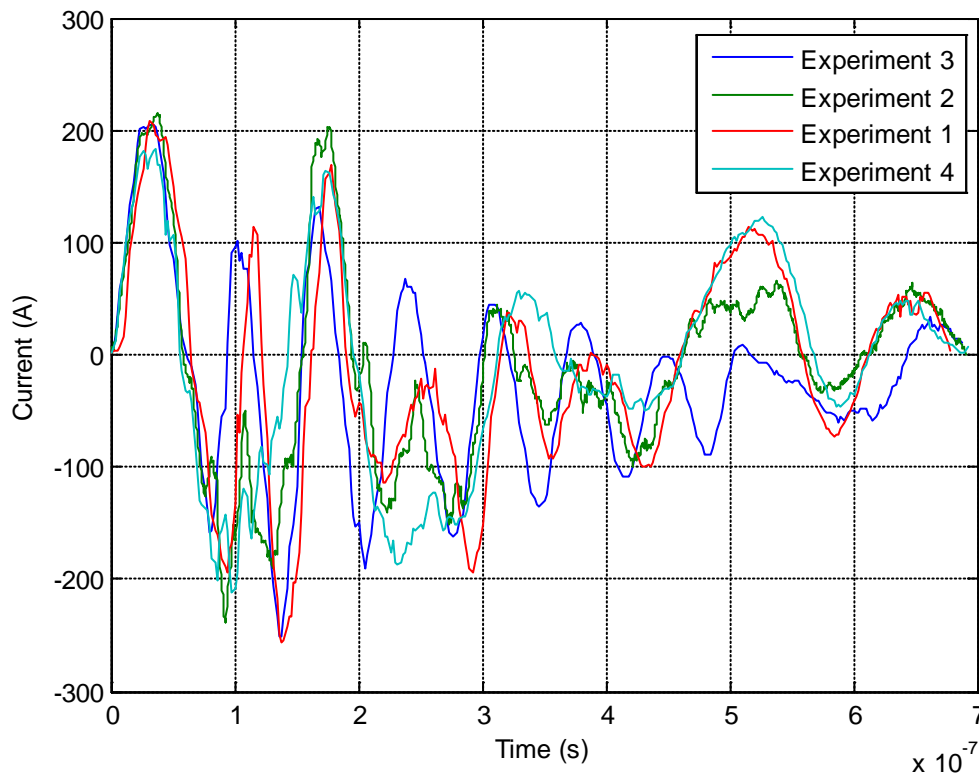


Figure 36. Combined plot for experiments 1-4 for 3" spark gap.

As an example, the general sine wave function is used to fit a curve to the first peak for experiment 1, and is shown in Figure 37. The R^2 value for this curve fit is 0.95.

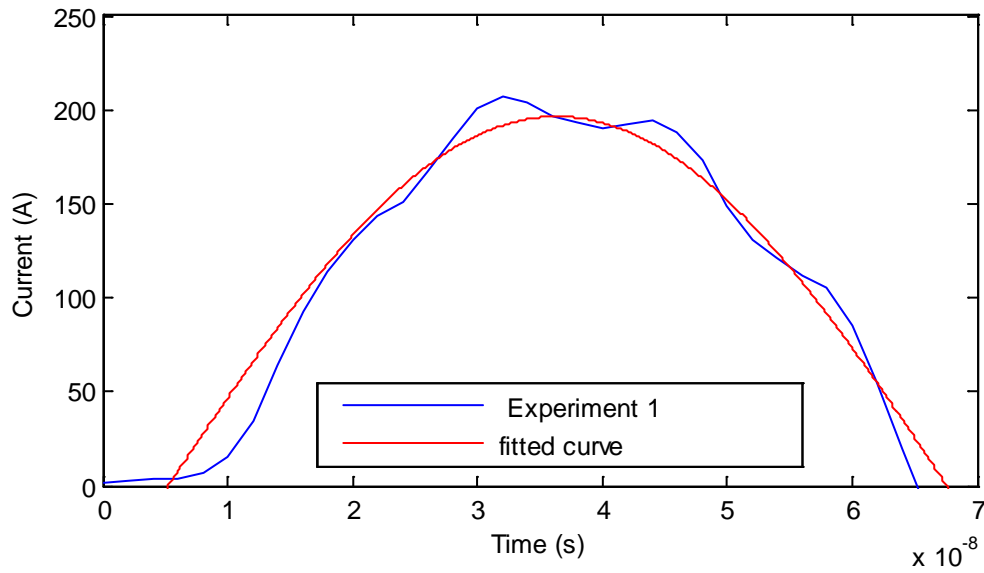


Figure 37. Curve fitted plot for the first oscillation for the data of experiment 1. The spark gap is 3".

3.5.4 Measurement of Current Amplitudes and Frequencies

The data measured with spark gaps of 3, 6, 7 and 8" were chosen to analyze the consistency of the spark system. The current amplitude of each first oscillation was analyzed using a sine function fit, and FFT was used to analyze the full current pulse for the dominate frequencies. The results are shown in Tables 14 through 17 with a summary in Tables 26.

Table 14. FFT frequencies for measurements made at a spark gap of 3"; first oscillation current amplitudes are also shown.

| Experiment | Current Amplitude of 1 st Oscillation | Primary Frequency (Hz) | Secondary Frequency (Hz) | Tertiary Frequency (Hz) |
|--------------------|--|------------------------|--------------------------|-------------------------|
| 1 | 207.6 | 2.96×10^6 | 1.48×10^7 | 6.90×10^6 |
| 2 | 214.5 | 7.00×10^6 | 2.90×10^6 | 1.48×10^7 |
| 3 | 204.4 | 1.50×10^7 | 1.00×10^6 | 7.00×10^6 |
| 4 | 182.5 | 6.99×10^6 | 2.99×10^6 | 2.40×10^7 |
| Mean Amplitude | | 202.25 | | |
| Standard Deviation | | 13.82 | | |

Table 15. FFT frequencies for measurements made at a spark gap of 6"; first oscillation current amplitudes are also shown.

| Experiment | Current Amplitude of 1 st Oscillation | Primary Frequency (Hz) | Secondary Frequency (Hz) | Tertiary Frequency (Hz) |
|--------------------|--|------------------------|--------------------------|-------------------------|
| 1 | 286.6 | 9.00×10^6 | 1.00×10^6 | 1.60×10^7 |
| 2 | 270.8 | 1.00×10^7 | 3.00×10^6 | 1.50×10^7 |
| 3 | 242.1 | 1.00×10^6 | 9.00×10^6 | 1.30×10^7 |
| 4 | 294.2 | 7.00×10^6 | 3.00×10^6 | 2.40×10^7 |
| Mean Amplitude | | 273.43 | | |
| Standard Deviation | | 23.05 | | |

Table 16. FFT frequencies for measurements made at a spark gap of 7"; first oscillation current amplitudes are also shown.

| Experiment | Current Amplitude of 1 st Oscillation | Primary Frequency (Hz) | Secondary Frequency (Hz) | Tertiary Frequency (Hz) |
|--------------------|--|------------------------|--------------------------|-------------------------|
| 1 | 323.8 | 8.00×10^6 | 1.00×10^6 | 1.50×10^7 |
| 2 | 311.3 | 8.00×10^6 | 3.00×10^6 | 1.50×10^7 |
| 3 | 273.3 | 1.00×10^6 | 1.50×10^7 | 8.00×10^6 |
| 4 | 346.1 | 7.00×10^6 | 3.00×10^6 | 2.40×10^7 |
| Mean Amplitude | | 313.63 | | |
| Standard Deviation | | 30.49 | | |

Table 17. FFT frequencies for measurements made at a spark gap of 8"; first oscillation current amplitudes are also shown.

| Experiment | Current Amplitude of 1 st Oscillation | Primary Frequency (Hz) | Secondary Frequency (Hz) | Tertiary Frequency (Hz) |
|--------------------|--|------------------------|--------------------------|-------------------------|
| 1 | 350.8 | 1.00×10^6 | 8.00×10^6 | 1.50×10^7 |
| 2 | 369.4 | 7.00×10^6 | 3.00×10^6 | 1.40×10^7 |
| 3 | 324.4 | 1.00×10^6 | 1.50×10^7 | 7.00×10^6 |
| 4 | 372.5 | 7.00×10^6 | 3.00×10^6 | 2.40×10^7 |
| Mean Amplitude | | 354.23 | | |
| Standard Deviation | | 22.10 | | |

Figure 38 shows that the first oscillation has the mean maximum current, as well as the mean frequency, rise as a function of spark gap distance. The rise is because current is a function of voltage and power. It takes more power to strike across longer distances; therefore current, voltage and frequency rise as spark gap distance is increased.

The 3" spark gap data resulted in the smallest standard deviation for current amplitude compared to 6, 7, and 8". The 3" spark gap resulted in currents with a mean value of 202.25 ± 13.82 (A) and rise to the 8" spark gap of 354.23 ± 22.10 (A). As shown in Tables 14-17. For the first three experiments the FFT data for the full current pulses produced three dominant frequency components of 3, 7 and 15 MHz \pm 2 MHz. The position of the primary to tertiary dominant frequencies changed, but all three days shared the same frequencies for the full wave. The FFT data for experiment 4 shared the 3 and 7 MHz \pm 2 MHz for all spark gaps, but its tertiary frequency was 24 MHz compared to the 15 MHz \pm 1.5 MHz, found on the three previous experiments.

Experiment 4 had higher humidity and temperature over the other three experiments, as shown in Table 13.

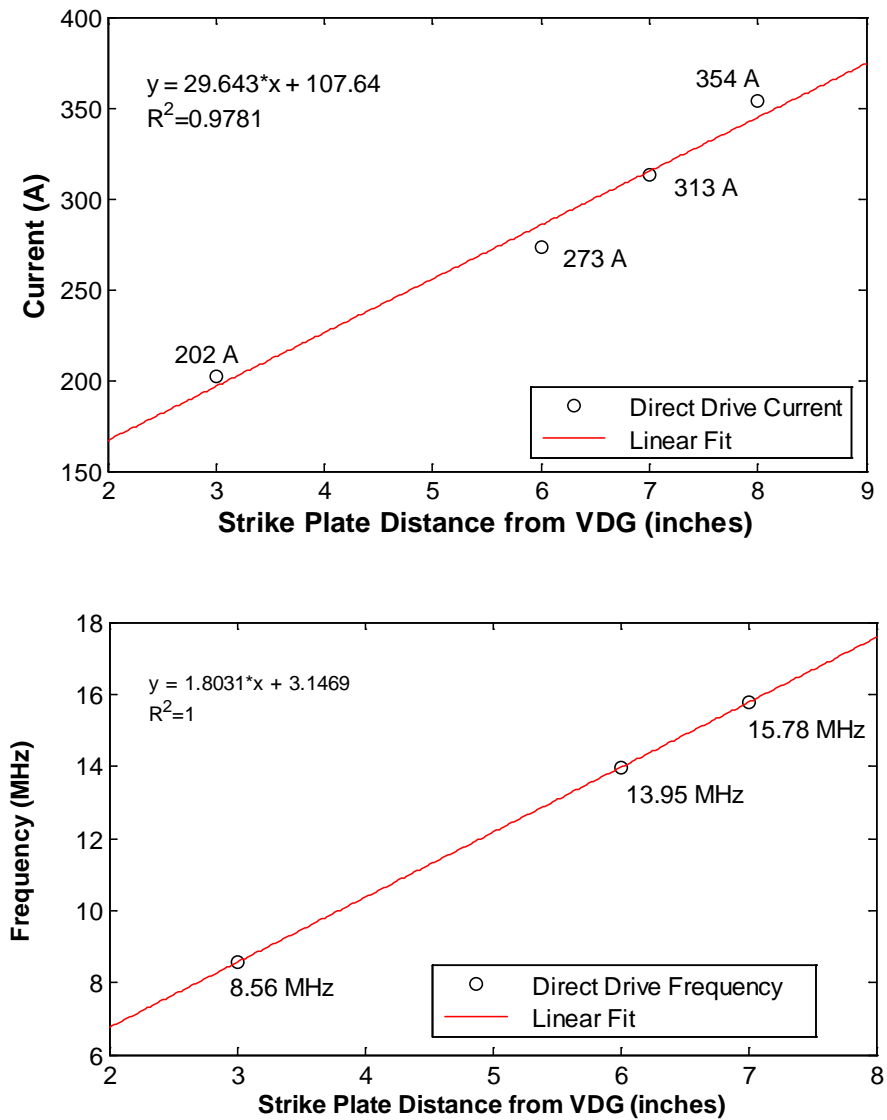


Figure 38. Direct drive current and frequency as a function of strike gap.

3.5.5 Curve Fitting of the First Oscillation

Curve fitting the data to the sine wave function of $I(t) = I_0 \sin[\omega t + \phi]$ is achieved by isolating the first oscillation from the rest of the data. The general models for the 3, 6, 7 and 8" spark gap distances, as well as the goodness of fit data for each distance, are shown in Tables 18-25 with a summary in Table 27. The curve fit for experiment 3, for a spark gap of 3", gave the best curve fit out of all of the spark gaps investigated, yielding an R^2 value 0.983, this is illustrated in Figure 39.

Table 18. Curve fit parameters for the first oscillations of current pulses measured with a spark gap distance of 3", for the general model of $I(t) = I_0 \sin[\omega t + \phi]$.

| Experiment | General Model Solution: $I(t) = I_0 \sin[\omega t + \phi]$ | | | 95% Confidence Bounds | | | | | |
|------------|--|---------------------|------------------|-----------------------|---------------|---------------------|---------------------|---------------|----------------|
| | | | | I_0 low | I_0 high | ω low | ω high | Φ low | Φ high |
| 1 | 196.4 sin[5.04x10 ⁷ t − 0.263] | | | 186.6 | 206.1 | 4.9×10 ⁷ | 5.2×10 ⁷ | -0.34 | -0.19 |
| 2 | 209.4 sin[5.51x10 ⁷ t − 0.104] | | | 206.6 | 212.1 | 5.5×10 ⁷ | 5.6×10 ⁷ | -0.13 | -0.08 |
| 3 | 201.7 sin[5.52x10 ⁷ t − 0.109] | | | 195.9 | 207.4 | 5.4×10 ⁷ | 5.6×10 ⁷ | -0.15 | -0.07 |
| 4 | 181.0 sin[5.46x10 ⁷ t − 0.097] | | | 173.8 | 188.2 | 5.3×10 ⁷ | 5.7×10 ⁷ | -0.16 | 0.04 |
| Mean | 197.1 sin[5.38x10 ⁷ t − 0.143] | | | 190.7 | 203.5 | 5.2×10 ⁷ | 5.5×10 ⁷ | -0.19 | -0.08 |
| Std Dev | $I_0 =$ 12 | $\omega =$ 2.3E6 | $\phi =$ 0.08 | 13.93 | 10.49 | 2.7×10 ⁶ | 2.0×10 ⁶ | 0.10 | 0.09 |

Table 19. Goodness of fit statistics for the first oscillation of current pulses measured with a spark gap distance of 3".

| Experiment | R^2 | SSE | Adjusted R^2 | RMSE |
|------------|-------|-------|----------------|-------|
| 1 | 0.950 | 9803 | 0.944 | 17.78 |
| 2 | 0.975 | 15760 | 0.974 | 10.69 |
| 3 | 0.983 | 2723 | 0.982 | 9.86 |
| 4 | 0.963 | 3761 | 0.961 | 12.03 |

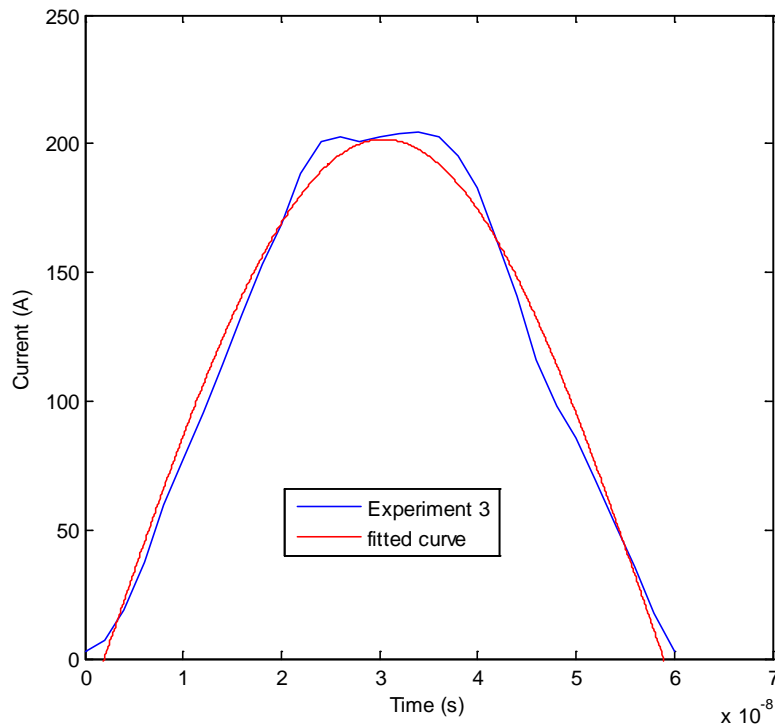


Figure 39. The best curve fit data was for experiment 3, and is for the spark gap of 3". This curve fit has an R^2 value of 0.983.

The 3" spark gap resulted in the best R^2 data over the 4 experiments. The average solution for the 3" spark gap over all four experiments is shown in Figure 40, along with the low current amplitude data point given on experiment 4 and the high current amplitude data point given on experiment 2. The averaged solution including the standard deviation is shown in Figure 41.

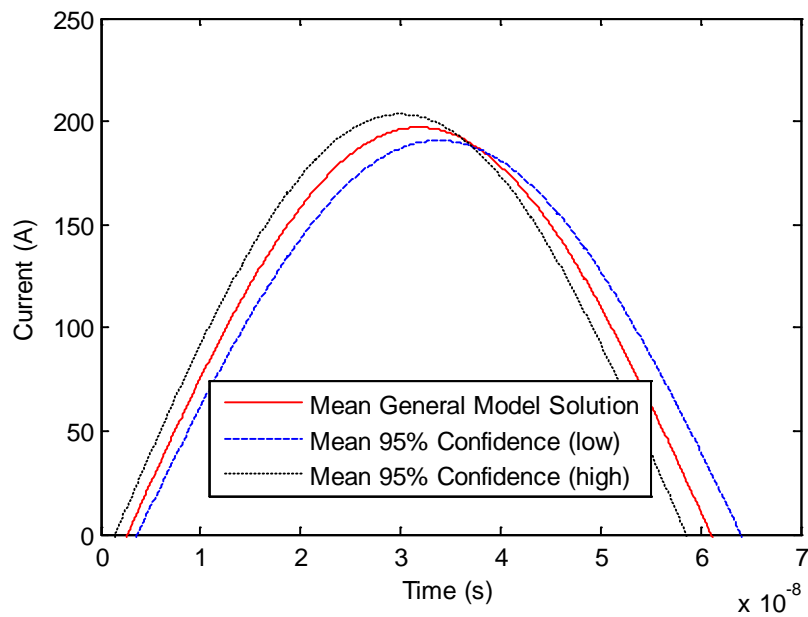


Figure 40. Curve fit to the first oscillation of the current pulse for a spark gap of 3'' along with the low and high current amplitudes are shown.

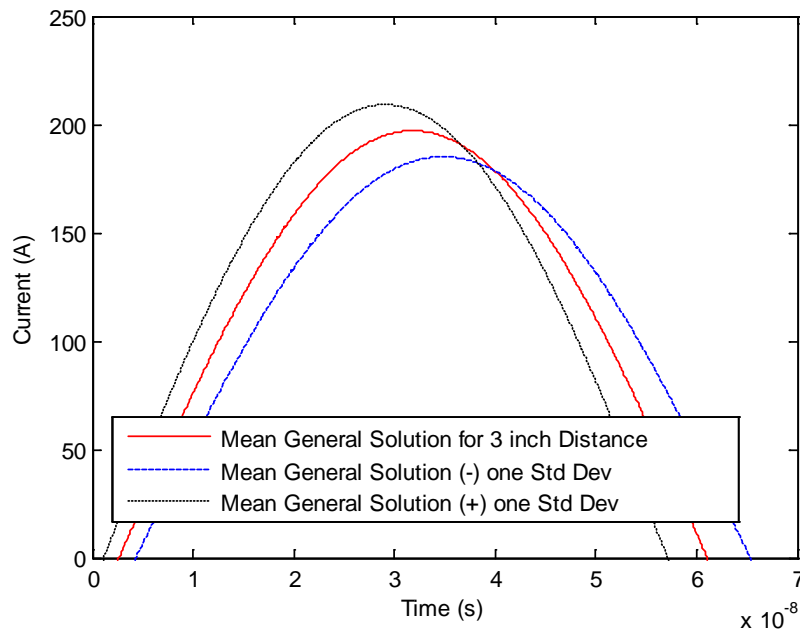


Figure 41. Curve fit to the first oscillation of the current pulse for a spark gap of 3'' along with the standard deviations are shown.

Table 20. Curve fit parameters for the first oscillations with a spark gap of 6'' for the general model of $I(t) = I_0 \sin[\omega t + \phi]$.

| Experiment | General Model Solution: $I(t) = I_0 \sin[\omega t + \phi]$ | | | 95% Confidence Bounds | | | | |
|------------|--|-----------------------------------|------------------|-----------------------|---------------|---------------------|---------------------|---------------------------|
| | | | | I_0 low | I_0 high | ω low | ω high | Φ low Φ high |
| 1 | 272.9 sin[9.24x10 ⁷ t - 0.052] | | | 252.9 | 292.8 | 8.7×10 ⁷ | 9.8×10 ⁷ | -0.06 0.17 |
| 2 | 251.0 sin[9.30x10 ⁷ t - 0.236] | | | 247.3 | 255 | 9.2×10 ⁷ | 9.4×10 ⁷ | -0.26 -0.21 |
| 3 | 212.1 sin[8.277x10 ⁷ t - 0.126] | | | 185.4 | 238.9 | 7.4×10 ⁷ | 9.1×10 ⁷ | -0.31 -0.06 |
| 4 | 237.5 sin[8.27x10 ⁷ t - 0.077] | | | 206.6 | 268.4 | 7.4×10 ⁷ | 9.1×10 ⁷ | -0.27 0.12 |
| Mean | 243.45 sin[8.77x10 ⁷ t - 0.123] | | | 223.1 | 263.8 | 8.2×10 ⁷ | 9.4×10 ⁷ | -0.23 0.02 |
| Std Dev | $I_0 =$ 25.4 | $\omega =$ 5.8×10 ⁶ | $\phi =$ 0.08 | 32.49 | 22.8 | 8.9×10 ⁶ | 3.1×10 ⁶ | 0.11 0.17 |

Table 21. Goodness of fit statistics for the first oscillation with a spark gap of 6''.

| Date | R ² | SSE | Adjusted R ² | RMSE |
|----------|----------------|--------|-------------------------|-------|
| 16/11/12 | 0.941 | 9471 | 0.941 | 25.13 |
| 17/11/12 | 0.937 | 1.80E5 | 0.937 | 23.14 |
| 29/11/12 | 0.871 | 2.21E4 | 0.855 | 36.04 |
| 4/12/12 | 0.856 | 2.94E4 | 0.856 | 41.56 |

Table 22. Curve fit parameters for the first oscillations with a spark gap of 7'' for the general model of $I(t) = I_0 \sin[\omega t + \phi]$.

| Experiment | General Model Solution: $I(t) = I_0 \sin[\omega t + \phi]$ | | | 95% Confidence Bounds | | | | |
|------------|--|------------------------------------|------------------|-----------------------|---------------|---------------------|---------------------|---------------------------|
| | | | | I_0 low | I_0 high | ω low | ω high | Φ low Φ high |
| 1 | 311 sin[9.24x10 ⁷ t - 0.116] | | | 286.4 | 335.5 | 8.7×10 ⁷ | 9.8×10 ⁷ | -0.23 0.02 |
| 2 | 301 sin[10.28x10 ⁷ t - 0.059] | | | 298.3 | 303.4 | 1.0×10 ⁸ | 1.1×10 ⁸ | -0.07 0.05 |
| 3 | 271 sin[10.91x10 ⁷ t - 0.009] | | | 263.4 | 278.7 | 1.1×10 ⁸ | 1.1×10 ⁸ | -0.03 0.05 |
| 4 | 295 sin[9.24x10 ⁷ t - 0.082] | | | 262.7 | 327.1 | 8.5×10 ⁷ | 1.0×10 ⁸ | -0.24 0.08 |
| Mean | 294.5 sin[9.92x10 ⁷ t - 0.067] | | | 277.7 | 311.2 | 9.5×10 ⁷ | 1.1×10 ⁸ | -0.14 0.04 |
| Std Dev | $I_0 =$ 17 | $\omega =$ 8.24×10 ⁶ | $\phi =$ 0.04 | 17.6 | 25.6 | 1.1×10 ⁷ | 6.2×10 ⁶ | 0.11 0.03 |

Table 23. Goodness of fit statistics for the first oscillation with a spark gap of 7".

| Experiment | R ² | SSE | Adjusted R ² | RMSE |
|------------|----------------|--------|-------------------------|-------|
| 1 | 0.943 | 1.44E4 | 0.935 | 31.02 |
| 2 | 0.980 | 7.39E4 | 0.980 | 15.01 |
| 3 | 0.992 | 893.5 | 0.991 | 8.63 |
| 4 | 0.894 | 2.48E4 | 0.879 | 40.63 |

Table 24. Curve fit parameters for the first oscillations with a spark gap of 8" for the general model of $I(t) = I_0 \sin[\omega t + \phi]$.

| Experiment | General Model Solution: $I(t) = I_0 \sin[\omega t + \phi]$ | | | 95% Confidence Bounds | | | | | |
|------------|--|----------------------------|------------|-----------------------|------------------------|---------------------|---------------------|----------|-----------|
| | | | | I ₀ low | I ₀ high | ω low | ω high | Φ low | Φ high |
| 1 | 326.5 sin[8.73x10 ⁷ t - 0.057] | | | 298.0 | 354.7 | 8.1×10 ⁷ | 9.3×10 ⁷ | -0.19 | 0.07 |
| 2 | 350.9 sin[10.3x10 ⁷ t - 0.076] | | | 348.0 | 353.7 | 1.0×10 ⁸ | 1.0×10 ⁸ | -0.09 | -0.06 |
| 3 | 315.1 sin[9.82x10 ⁷ t - 0.098] | | | 298.0 | 332.0 | 9.4×10 ⁷ | 1.0×10 ⁸ | -0.18 | -0.02 |
| 4 | 321.5 sin[9.24x10 ⁷ t - 0.089] | | | 288.2 | 354.8 | 8.5×10 ⁷ | 1.0×10 ⁸ | -0.24 | 0.06 |
| Mean | 328.5 sin[9.52x10 ⁷ t - 0.080] | | | 308.1 | 348.8 | 9.1×10 ⁷ | 1.0×10 ⁸ | -0.17 | 0.01 |
| Std Dev | I ₀ = 15.6 | ω = 6.8×10 ⁶ | φ = .02 | 27.0 | 11.21 | 9.5×10 ⁶ | 4.7×10 ⁶ | 0.06 | 0.07 |

Table 25. Goodness of fit statistics for the first oscillation with a spark gap of 8".

| Experiment | R ² | SSE | Adjusted R ² | RMSE |
|------------|----------------|--------|-------------------------|-------|
| 1 | 0.930 | 2.17E4 | 0.921 | 36.8 |
| 2 | 0.981 | 8.63E4 | 0.981 | 16.47 |
| 3 | 0.972 | 6190 | 0.968 | 21.03 |
| 4 | 0.903 | 2.66E4 | 0.890 | 42.08 |

Table 26. Summary of the maximum current of the first pulse as a function of spark gap.

| Spark Gap(inches) | Max Current Mean/Average (amps) | Standard Deviation (amps) |
|-------------------|---------------------------------|---------------------------|
| 3 | 202.25 | 13.82 |
| 6 | 273.43 | 23.05 |
| 7 | 313.63 | 30.49 |
| 8 | 354.23 | 22.10 |

Table 27. Summary of the average parameters for the first current oscillations as a function of spark gap distance.

| Spark Gap(inches) | General Model Mean/Average Solution: $I(t) = I_0 \sin[\omega t + \phi]$ | Standard Deviation | | |
|-------------------|--|--------------------|----------------------------|---------------|
| | | I_0 | ω | Φ |
| 3 | $197.1 \sin[5.38 \times 10^7 t - 0.143]$ | $I_0 = 12$ | $\omega = 2.3 \times 10^6$ | $\phi = 0.08$ |
| 6 | $243.45 \sin[8.77 \times 10^7 t - 0.123]$ | $I_0 = 25.4$ | $\omega = 5.8 \times 10^6$ | $\phi = 0.08$ |
| 7 | $294.5 \sin[9.92 \times 10^7 t - 0.067]$ | $I_0 = 17$ | $\omega = 8.2 \times 10^6$ | $\phi = 0.04$ |
| 8 | $328.5 \sin[9.52 \times 10^7 t - 0.080]$ | $I_0 = 15.6$ | $\omega = 6.8 \times 10^6$ | $\phi = 0.02$ |

3.6 Results of Added Circuit Resistance

As shown in Section 2.4, the overdamped or critically damped RLC circuit current waveform best fits the free-field MIL-STD 464 standard test pulse. The critical resistance in damping the VDG system is the spark gap resistance $R_s(t)$, as shown in Equation (15). This controlling resistance has three independent variables. They are the air density (before air breakdown), length of the spark gap, and the time-dependent

current of the spark gap. It is this time dependent current that causes $R_s(t)$ to decrease with time.

The current in the spark gap cannot be measured directly, and the air density in the VDG room cannot be easily modified, such as was done with gas pressure in [5]. Thus, the best variable for achieving an overdamped RLC circuit in this research was to increase the spark gap resistance $R_s(t)$, via the spark gap or increasing the circuit resistance.

The data in Section 3.5.4 showed that the mean current increased as a function of spark gap distance from 202 to 354 (A) as the spark gap length increased from 3 to 8", as shown in Figure 38. However, in all experiments the increased spark gap did not increase $R_s(t)$ to the point of taking the VDG from the underdamped RLC circuit to overdamped.

A repeatable current was not obtained past 8". Larger spark gaps lead to erratic behavior owing to different spark paths/lengths, and eventually no strikes will occur. It was found that to have a repeatable current waveform, the spark gap was limited to 8". Strikes were measured up to 18"; however, those strikes only occurred once or twice before the strikes ceased altogether. To bring the strikes back, a much smaller spark gap was needed. The strikes past 9" were never repeatable; therefore, the distances of 3, 6, 7 and 8" were used to characterize the direct current from the VDG. At these distances, the VDG produced an underdamped waveform to the RLC circuit.

In an attempt to overdamp the VDG RLC circuit, ceramic resistors were added in series with the CVR, as shown in Figure 34. The method was predicated upon the theoretical analysis of Section 2.4. This section describes that in order to determine the

resistance needed to over damp the first oscillation in the current waveform is when

$$R^2 > 4L/C.$$

Since the first oscillation has a measured frequency of $8.56 \text{ MHz} \pm 0.37 \text{ MHz}$, for the spark gap of 3" (53.8 MHz for angular frequency), and using a capacitance of 45pF [6], as well as assuming the system is in resonance, the inductance was determined using $L = \frac{1}{\omega^2 C}$, yielding $9 \times 10^{-6} \text{ H}$. Solving for R, gives a value of 882Ω or greater.

Therefore, a 1 k Ω resistor was placed in series with the CVR.

The 1 k Ω resistor, however, caused an observable spark to jump past the resistor, obviously leading to high voltage build up just prior to the resistor. Aside from reducing the effect of the resistor, it occasionally short circuited the oscilloscope causing it to cycle off. When the oscilloscope did not short circuit, the measurements varied in amplitude and frequency with every strike. Resistors ranging from 10 to $10^6 \Omega$ were used, but none could be used without causing the breakdown of air around the resistor and thus would not overdamp the VDG.

Resistors, smaller than 1 k Ω , did produce measurable data, such as that for a 692 Ω resistor, as shown in Figure 42. However, in all cases, the second oscillation was measured to have a higher maximum current than the first. This was likely caused by constructive interference from a reflection caused by the placement of the resistor. The first peaks also had added wave features, as shown in Figure 43.

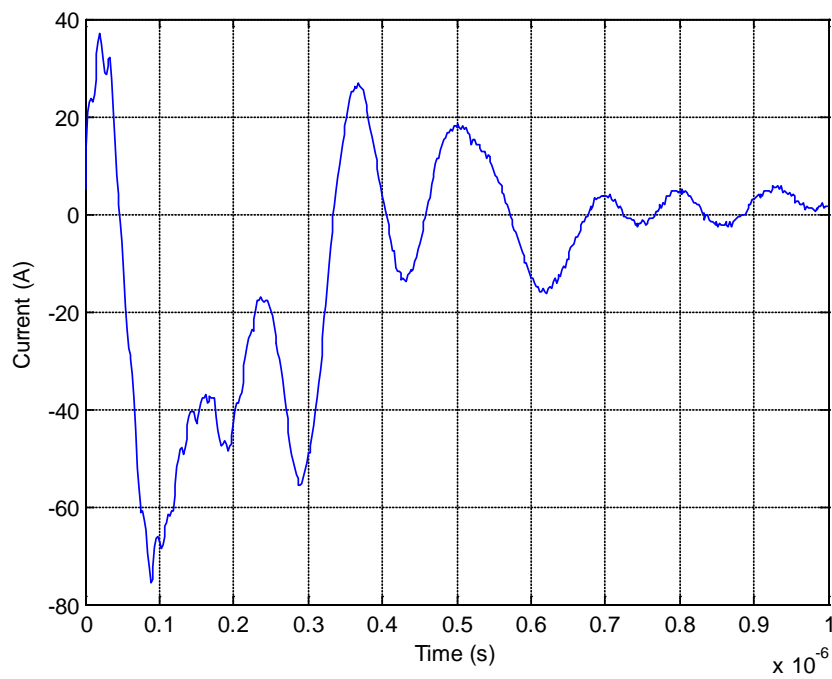


Figure 42. Current as a function of time measured with a resistor of $692\ \Omega$ added in series with the CVR.

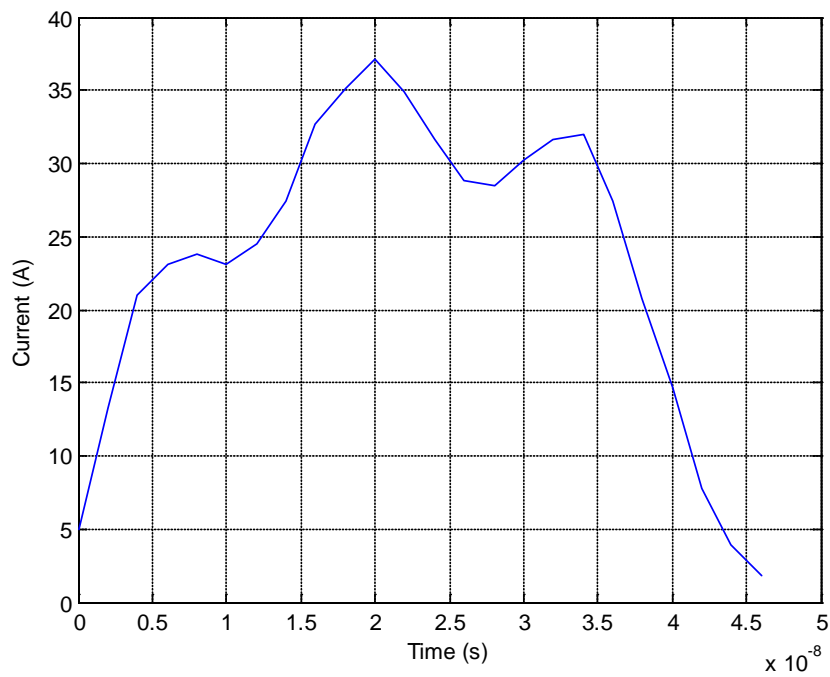


Figure 43. First oscillation of the current pulse measured with a resistor of $692\ \Omega$ added in series with the CVR.

CHAPTER 4

CONCLUSIONS

4.1 Confidence in the Equipment and CVR Location

The equipment used to measure the direct current of the VDG indicated that the aluminum shielded coaxial cables, CVR, and oscilloscope were functioning properly, and that they are capable of measuring the currents and current signals at frequencies expected of the VDG. Losses in the lines and connections appeared to be minimal, but the effect on the outcome of the final waveforms appears to induce reflections that could not be removed.

The use of the RG-62 shielded coaxial cable that was terminated at $10^6 \Omega$ at the oscilloscope and a 100Ω shunt terminator gave the least noisy signal and produced the highest current amplitude, as shown in Table 12. It was also shown in Table 12 that the signal noise was reduced when the CVR is connected at position A, as shown in Figure 30, and when copper mesh clamps are used. This setup was used throughout all the repeatable experiments.

4.2 VDG Experimental Setup

All experimental VDG discharge data produced a waveform with at least 3 FFT frequency components: 3, 7, 15 MHz \pm 2 MHz. The primary frequency, at ~15MHz, is a result of the capacitance and inductance of the VDG resonating with the channel inductance [12]. The additional frequency components are created by electromagnetic interference and cable interference (inductance and capacitance.)

It was found that placement of the 30' RG-62 shielded coaxial cable, as shown in Figure 28, changed the current pulse by up to 117 (A). In addition, the RG-62 shielded coaxial cable, and all power and ground cables had to be supported off the concrete floor so as to eliminate any ground current coupling. It was also shown that a poor CVR attachment can lead to added frequencies of oscillation in the current pulse. In other words, the CVR connection, including the placement of the RG-62 cable, is critical in eliminating any additional impedance differences and in producing repeatable current strikes with the first oscillation having the maximum peak current.

4.3 Analysis/Repeatability of the First Current Oscillations

Repeatable and reliable direct current amplitude and frequency were measured and found for only the first current oscillation. Therefore, at this time EMP direct current survivability testing cannot be conducted by the VDG.

The VDG represents an underdamped RLC circuit that is controlled by the dielectric breakdown of air. In an ideal RLC circuit, the VDG would produce a damped sine wave as modeled in Section 2.4.1. It was found that with many manipulations the ideal could not be achieved. However, the first oscillation of the current pulse can be repeated to within a small statistical variance outlined in Tables 26 and 27 and could be used for initial EMP verification of whether subcomponents should be MIL-STD tested.

4.4 Added Resistance to Obtain a Damped Current Waveform

Prior studies have shown that damping of the oscillations of a VDG is best controlled by raising the gas pressure [5]. However, it is not practicable under the current configuration. Owing to the requirement for air breakdown, the spark gap was limited to 8" in these experiments; therefore, $R_s(t)$ was not increased enough to attain the overdamped RLC circuit.

The series resistance experiments resulted in direct current that was prone to jumping any added resistors. Therefore, reliable and repeatable data could not be obtained through this method.

CHAPTER 5

FUTURE WORK

5.1 VDG System Improvements

The EMI found in the VDG room affected all the results for all experiments. The room is full of conductive materials that add to the electromagnetic mode of the VDG system. Changing the room or the room environment is advisable. This could be done by adding a Faraday cage around the VDG or adding electromagnetic absorbent material onto the walls.

To maximize the impedance matching of the spark gap, a strike plate should be constructed to equal the capacitance of the VDG dome. This strike plate would then need to be supported far from the concrete floor in order to reduce the capacitance. To further eliminate additional EMI caused by impedance miss-matches and connections, a permanent connection of the CVR should be made. This could be done by soldering the CVR into a fixed location. And finally, to eliminate current coupling with the RG-62 cable a permanent non-conducting support structure or a permanent copper tubing to hold the coaxial cable should be emplaced.

5.2 Follow-on Experiments

Subcomponents that did not undergo direct current EMP testing could be preliminarily evaluated against the direct current produced by the VDG. The VDG produces current pulses with frequency components that are spark gap distance dependent. With the spark gap ranging from 3 to 8" there was a current amplitude produced that ranged from 202 to 350 (A), as well as a frequency range of 8 to 15 MHz.

This initial evaluation would be to ensure the subcomponents meet or do not meet initial direct current EMP military standard requirements. If they do not pass the VDG direct current evaluation the subcomponents could be recommend for MIL-STD testing. For this evaluation to be validated the VDG would need to be setup and tested to make sure that the first current oscillation is the maximum peak for the full current pulse. And finally, the VDG could be used to provide a quick analysis of suspected vulnerable components, as well as for EMP and static discharge education.

APPENDIX A– VDG Triboelectric Effect and Solution to DEQ

VDG Triboelectric Effect

If used without the 20 kV voltage source, the VDG can take advantage of the theory pertaining to charging by the triboelectric effect and induction if the belt material is lower on the triboelectric scale than the lower roller material. An example is with a rubber belt and a plastic roller, then the belt will carry excess negative charge where it is in contact with the roller and the roller will carry excess positive charge, as shown in Figure 44. Materials could also be chosen to invert these charges. Since the belt surface area is far greater than the roller surface area, the surface charge density will be far greater on the roller than on the belt.

Acting through the belt, the strongly positive charged roller creates a strong electric field from the roller to the negatively charged metal comb. The lesser negative charge density, on the inside of the belt, partially shields and reduces the dominant effects of the roller's high density charge from the negatively charged comb. At the same time, the metal comb with the tips of its tines very near to the lower roller is electrically continuous with ground. This is shown in Figure 45.

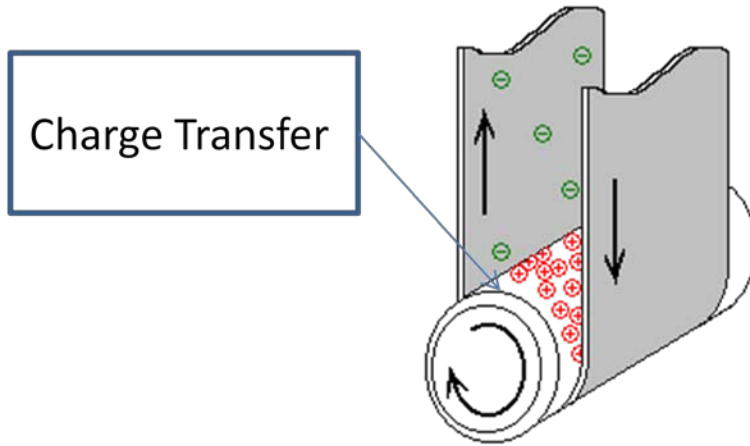


Figure 44. Charge density is greater on the roller than the inside of belt. Adapted from [8].

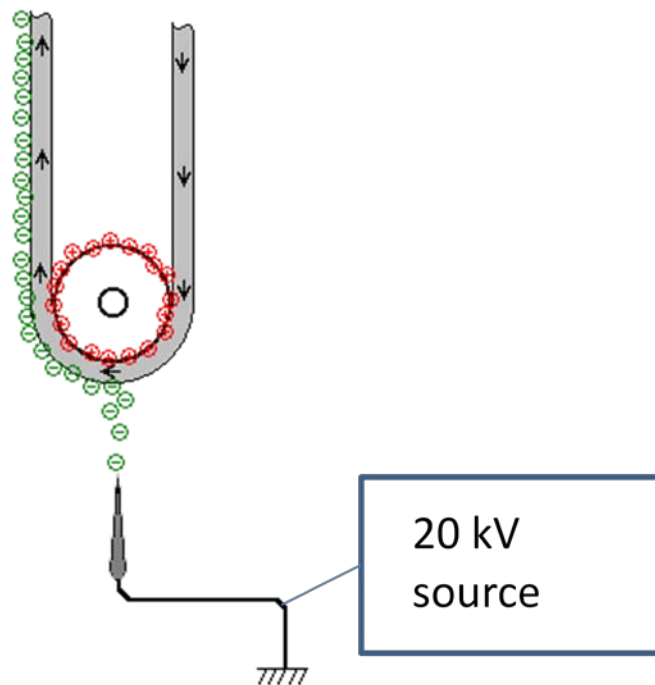


Figure 45. High field strength ionizes the air gap to allow charge transport. Adapted from [8].

The charge on the roller is much more concentrated than the charge on the belt. Because of this difference in charge concentration, the roller's electric field is much

stronger than the belt's at the location of the roller and lower comb assembly. The strong positive charge from the roller begins to do two things:

1. It attracts the electrons near the tips of the lower comb assembly. Metals are good conductors because they are basically positive atoms surrounded by movable electrons. The comb assembly has wire tips that are negatively charged because the electrons have moved to the tips of the comb.
2. It begins to strip nearby air molecules of their electrons. The VDG now has free electrons and positively charged atoms of air existing between the roller and the comb. The electrons are attracted to the roller and repelled from the comb tips while the positive atoms are repelled from the positively charged roller.

The negatively charged electrons from the air molecules are drawn toward the positively charged roller, but the belt is in the way; therefore, the belt gets "coated" with the negative charge, which it then carries away from the roller.

As long as there is air between the lower roller and comb assembly, the VDG will continue to charge the belt. Theoretically, the VDG can continue to charge and is only limited by the volume of the dome/capacitor.

As soon as electrons accumulate on the belt it is negatively charged. The electrons now roll toward the upper roller and upper comb assembly. Since the upper roller is made of a material that will repel the charge on the belt, and the upper comb assembly is connected to the inside of the dome, the electrons on the belt move to the tips of the metal comb as they are repelled by the now negatively charged top roller. Once again the air breaks down between the comb and belt (just like the bottom roller), and the positive atomic nuclei of air are attracted to the roller, and at the same time, the free

electrons in the air move to the comb. When a charged object touches the inside of the metal container, the container accepts the charge, leaving the object neutral. The excess charge then shows up on the outside surface of the dome, now making it a large capacitor. It is through this effect that the VDG is able to achieve large voltage and electric field.

Solutions to the RLC Differential Equation

The MIL-STD-464 is a single pulse (with a fast rise time, and an order of magnitude longer fall time), while the VDG gives an oscillating sinusoidal wave. To better simulate a free field EMP pulse, the RLC circuit of the VDG needed to be overdamped or critically damped. The solutions to the second-order linear differential equation with constant coefficients, as outlined for the RLC circuit, are summarized in Table 28 [18].

The RLC second order linear differential equation is given in its general form in Equation (26):

$$a \frac{d^2 y}{dt^2} + b \frac{dy}{dt} + cy = 0, \quad (26)$$

and has the characteristic equation of Equation (27).

$$ar^2 + br + c = 0 \quad (27)$$

This characteristic equation is a quadratic formula and gives rise to three different general solutions for the homogenous solution (y_h) for the differential Equation (9).

These solutions depend on the value of the discriminate ($\Delta = b^2 - 4ac$), where b equals R, α equals L, and c equals 1/C for the RLC circuit. The solutions to these equations show that the overdamped or critically damped solutions are in the general form of MIL-STD-464.

Since b equals the resistance R in the circuit, and it is squared, the resistance is the dominant factor in determining the discriminator and whether the solution is underdamped or overdamped. A comparison of these three different solutions is shown in Figure 10 [18].

Table 28. Solution to the second-order linear differential equation with constant coefficients is shown. Adapted from [18].

| | | |
|------------------------|---|--|
| Case 1 $\Delta > 0$ | Real unequal roots: $r_1, r_2 = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ | Over damped motion: $y_h = c_1 e^{r_1 t} + c_2 e^{r_2 t}$ |
| Case 2 $\Delta = 0$ | Real repeated root: $r = \frac{-b}{2a}$ | Critically damped motion: $y_h = c_1 e^{rt} + c_2 t e^{rt}$ |
| Case 3 $\Delta < 0$ | Complex conjugate roots: $r_1, r_2 = \alpha \pm \beta i$ $\alpha = \frac{b}{2a}, \beta = \frac{\sqrt{4ac - b^2}}{2a}$ | Under damped motion: $y_h = e^{\alpha t} (c_1 \cos \beta t + c_2 \sin \beta t)$ |

APPENDIX B – Additional Equipment Confidence Experiments

Equipment Confident Experiments:

The Signal source was connected straight into the oscilloscope with an RG 62/U cable that was terminated with a 100 Ω shunt terminator. This data shows that with the 100 Ω shunt terminator V_L is higher on the oscilloscope due to the fact that the 100 Ω shunt terminator in parallel with the 93 Ω cable has a total impedance of 48 Ω , and a constructive reflection is added to the V_L .

Table 29. Voltage Load (V_L) is higher when shunt terminators are used. This is because of constructive impedance reflections.

| Signal Source (50 Ω impedance) | | Oscilloscope (Terminated at 1M Ω) with RG-62 (93 Ω) cable of 3ft length | | Oscilloscope (Terminated at 1M Ω) with RG-62 (93 Ω) cable of 20 ft length | |
|--|---------|--|---------|--|---------|
| Frequency | Voltage | Frequency | Voltage | Frequency | Voltage |
| 1 MHz | 1 V | 1 MHz | 1.33V | 1 MHz | 1.33V |
| 1 MHz | 5 V | 1 MHz | 6.68 V | 1 MHz | 6.60 V |
| 1 MHz | 10 V | 1 MHz | 13.44 V | 1 MHz | 13.36 V |
| 1 MHz | 5 V | 1 MHz | 6.68 V | 1 MHz | 6.60 V |
| 10 MHz | 5 V | 10 MHz | 6.72 V | 10 MHz | 6.72 V |
| 15 MHz | 5 V | 15 MHz | 6.88 V | 15 MHz | 6.52 V |
| 20 MHz | 5 V | 20 MHz | 6.96 V | 20 MHz | 6.56 V |

With the CVR placed at position A it is shown that resonance is reached at 15 MHz. This is known because the voltage reaches a maximum at this frequency.

Table 30. When CVR is placed in position A resonance is approached around 15 MHz, as maximum voltage is obtained.

| Signal Source (50 Ω impedance) | | With CVR Oscilloscope (Terminated at 1M Ω and a 100 Ω shunt terminator placed in parallel) | |
|--|---------|---|---------|
| Frequency | Voltage | Frequency | Voltage |
| 1 MHz | 5 V | 1 MHz | 6.8 mV |
| 1 MHz | 10 V | 1 MHz | 11.2 mV |
| 10 MHz | 5 V | 10 MHz | 13.6 mV |
| 11 MHz | 5 V | 10 MHz | 14.4 mV |
| 12 MHz | 5 V | 12 MHz | 7.8 mV |
| 13 MHz | 5 V | 13 MHz | 9.6 mV |
| 14 MHz | 5 V | 14 MHz | 23.0 mV |
| 15 MHz | 5 V | 15 MHz | 32.0 mV |
| 16 MHz | 5 V | 16 MHz | 24.0 mV |
| 17 MHz | 5 V | 17 MHz | 16.0 mV |
| 18 MHz | 5 V | 18 MHz | 16.0 mV |
| 19 MHz | 5 V | 19 MHz | 7.6 mV |
| 20 MHz | 5 V | 20 MHz | 6.2 mV |

The experiment system was again set up by connecting the voltage source to the front of the strike plate using alligator clips and copper foil tape. This time the CVR was attached near the very back of the strike plate. The experiment was run to show how the

added impedance of the strike plate affects the experiment results. Comparing this data to Table 12 it is shown that a better impedance match is made at position A then at the back of the strike plate.

When the actual VDG experiments were run it also showed that placing the CVR at the very back of the strike plate added additional high frequencies and the ability to reproduce the current form was almost impossible. Therefore, position A was again shown to be the cleaner CVR location.

Table 31. Experiment data with CVR placed at the very back of the strike plate.

| Signal Source (50 Ω impedance) | | Without CVR (The oscilloscope was terminated at 50 Ω , RG-62 cables were used) | | With CVR (The oscilloscope was terminated at 50 Ω , RG-62 cables were used) | |
|--|---------|--|---------|---|---------|
| Frequency | Voltage | Frequency | Voltage | Frequency | Voltage |
| 1 MHz | 1 V | 1 MHz | 0.8 V | 1 MHz | 0.04 A |
| 1 MHz | 5 V | 1 MHz | 4.1 V | 971 kHz | 0.15 A |
| 1 MHz | 10 V | 1 MHz | 8.9 V | 1 MHz | 0.30 A |
| 1 MHz | 5 V | 1 MHz | 4.3 V | 992 kHz | 0.17 A |
| 10 MHz | 5 V | 10 MHz | 2.6 V | 10 MHz | 0.11 A |
| 15 MHz | 5 V | 15 MHz | 3.9 V | 14.95MHz | 0.12 A |
| 20 MHz | 5 V | 20 MHz | 3.8 V | 20 MHz | 0.13 A |

APPENDIX C – Goodness of Fit and Computer Codes

Goodness of Fit and Mathematical Algorithm and MATLAB Codes Used:

Goodness of Fit

Sum of Squares Due to Error:

This statistic measures the total deviation of the response values from the fit to the response values. It is also called the summed square of residuals and is usually labeled as SSE, as shown in Equation (28). A value closer to 0 indicates a better fit.

$$SSE = \sum_{i=1}^n \omega_i (y_i - \widehat{y_i})^2 \quad (28)$$

R-Square:

This statistic measures how successful the fit is in explaining the variation of the data. Put another way, R-square is the square of the correlation between the response values and the predicted response values. It is also called the square of the multiple correlation coefficient and the coefficient of multiple determination.

R-square is defined as the ratio of the sum of squares of the regression (SSR) and the total sum of squares (SST). SSR is defined in Equation (29).

$$SSR = \sum_{i=1}^n w_i (\widehat{y_i} - \bar{y})^2 \quad (29)$$

SST is also called the sum of squares about the mean, and is defined in Equation (30),

$$SST = \sum_{i=1}^n \omega_i (y_i - \bar{y})^2, \quad (30)$$

where $SST = SSR + SSE$. Given these definitions, R-square is expressed in Equation (31).

$$R^2 = \frac{SSR}{SST} = 1 - \frac{SSE}{SST} \quad (31)$$

R-square can take on any value between 0 and 1, with a value closer to 1 indicating a better fit. For example, an R^2 value of 0.8234 means that the fit explains 82.34% of the total variation in the data about the average.

If you increase the number of fitted coefficients in your model, R-square might increase although the fit may not improve. To avoid this situation, you should use the degrees of freedom adjusted R-square statistic described below.

Note that it is possible to get a negative R-square for equations that do not contain a constant term. If R-square is defined as the proportion of variance explained by the fit, and if the fit is actually worse than just fitting a horizontal line, then R-square is negative. In this case, R-square cannot be interpreted as the square of a correlation.

Degrees of Freedom Adjusted R-Square:

This statistic uses the R-square statistic defined above, and adjusts it based on the residual degrees of freedom. The residual degrees of freedom is defined as the number of response values n minus the number of fitted coefficients m estimated from the response values $v = n - m$ where v indicates the number of independent pieces of information involving the n data points that are required to calculate the sum of squares. Note that if parameters are bounded and one or more of the estimates are at their bounds, then those estimates are regarded as fixed. The degree of freedom is increased by the number of such parameters.

The adjusted R-square statistic is generally the best indicator of the fit quality when you add additional coefficients to your model, as shown in Equation (32):

$$\text{adjusted } R^2 = 1 - \frac{SSE(n-1)}{SST(v-1)} \quad (32)$$

The adjusted R-square statistic can take on any value less than or equal to 1, with a value closer to 1 indicating a better fit.

Root Mean Squared Error:

This statistic is also known as the fit standard error and the standard error of the regression, as shown in Equation (33),

$$RMSE = s = \sqrt{MSE} , \quad (33)$$

where MSE is the mean square error or the residual mean square, as shown in Equation (34):

$$MSE = \frac{SSE}{v} \quad (34)$$

A $RMSE$ value closer to 0 indicates a better fit.

MATLAB Codes:

The Fast Fourier Transform (FFT) is an algorithm to compute the Discrete Fourier Transform (DFT) and its inverse. The MATLAB code used for this is shown:

```
clear
Data=importdata('File Name for data set.xls')
X=Data(:,1);
Y=Data(:,2);
```

```

dt=mean(diff(X));
nyquist=1/(2*dt);
n=length(Y);
freq=(1:n/2)./(n/2).*nyquist;

ffty=fft(Y);
ffty=abs(ffty.^2);
plot(freq,ffty(1:length(Y)/2))

```

Computer model for the iterative time dependent spark gap current:

```

close all
clear all
clc
want_to_save=true;

%Variable to Change --- Maybe
dt=1e-11;% seconds - - time steps
tmax=1e-6; % seconds - - time max
inch = 3; % inches - - variable Spark Gap distance changes other
variables
c =200*10^(-12); %Farads 45 from Leahy's work
L = 370e-9; % (1.4*10^(-9)/.03937)*(inch);%Henrys from Charlesworth
Research
ScaledAmplitude = 207; % from real data information to normalize from
Spark Gap current to direct current

t=0:dt:tmax; % time start at 0 to tmax
l = (.0254/1)*(inch);% conversion of spark gap distance from inches to
meters
V0 = (2.9*10^(6)*(.0254/1)*(inch));% V/m (m) - - air breakdown voltage
divided by Spark Gap distance to get voltage
rho = 1.225 ;%kg/m^3 for 1 atmosphere before break down
%%

It=0; % initial conditions at time zero

Itdt=1e-9; % initial conditions at time zero - - can not divide by zero

jj=0; % initialize index

h=waitbar(0); % to add the waitbar :)
res=zeros(size(t)); % initializing the array with zeros to same size
as t
Itval=res; % initializing Itval - same as res
Itdtval=res; % initializing Itval - same as res
for tt=t % looping thru for steps of t
    jj=jj+1;
    waitbar(tt/tmax,h)

    Itdt=Itdt+It^(2/3)*dt; % approximation of the integral - - the
smaller the dt the smaller the error but longer the time - for 45pF we
max out at 1E-11

```

```

        resistance=((7e-4*rho^(1/3)*1)./(Itdt)); % Spark Gap Resistance
defined - - update for each iteration using the previous iteration
        w0=sqrt(1/(L*c)-(resistance/(2*L))^2); % angular frequency defined
        It=V0/(w0*L)*exp(-resistance/(2*L)*tt)*sin(w0*tt); % Time dependent
current defined

        res(jj)=resistance; % storing the array of resistance
        Itval(jj)=It; % storing the current array
        Itdtval(jj)=Itdt; % storing the integral values
end

close(h) % close the waitbar :)

%%
% Plots of the figures - - each defined below
Scaled_Output=figure(1);
hold on
plot(t,real(Itval)/max(real(Itval))*ScaledAmplitude,'r') %
Scaled/normalized current
set(gcf,'position',[644 676 560 420])

figure(5)
plot(t,real(Itval)) % current
set(gcf,'position',[50 676 560 420])

figure(2)
loglog(t/1e-9,real(res)); % resistance
set(gcf,'position',[1235 676 560 420])

figure(3)
for ii=2:length(Itdtval)
    Integralerror(ii-1)=abs((Itdtval(ii)-Itdtval(ii-1))/Itdtval(ii));
end
plot(Integralerror)
set(gcf,'position',[50 99 560 420])
figure(4)
plot(t,real(Itdtval)); % Current Integral for resistance
set(gcf,'position',[644 99 560 420])

figure(1)

if want_to_save
uisave({'Itval','L','V0','c','dt','inch','l','rho','t'},'DataOut')
end

```

Mathematica Codes

The mathematica computer model used to manipulate data for a damped sin wave is shown:

Identify to *Mathematica* the directory where data are stored.

```
SetDirectory["L:\\Research\\ENP\\GNE Research\\EMP Research\\Kress\\MMA
```

```
Curve Fitting"];
```

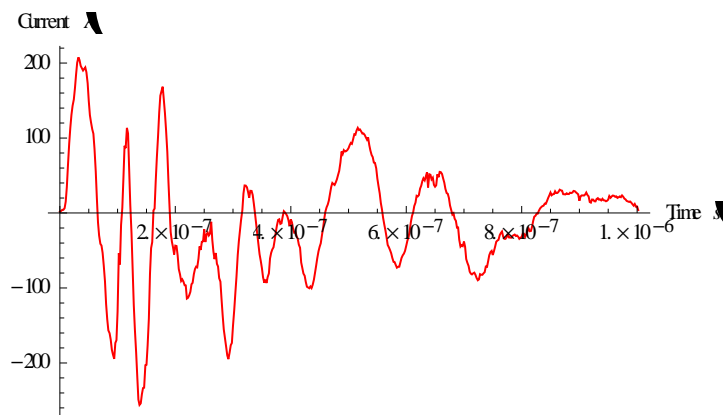
Import data and remove the extra dimension generated by Mathematica.

```
plotData=Flatten[Import["16 Nov 2012 Full Pulse.xlsx","XLSX"],1];
```

Take a first look at the data.

```
dataPlot=ListPlot[plotData,Joined→True,PlotRange→All,PlotStyle→Red,AxesLab
```

```
el→{Time[s], Current[A]}]
```

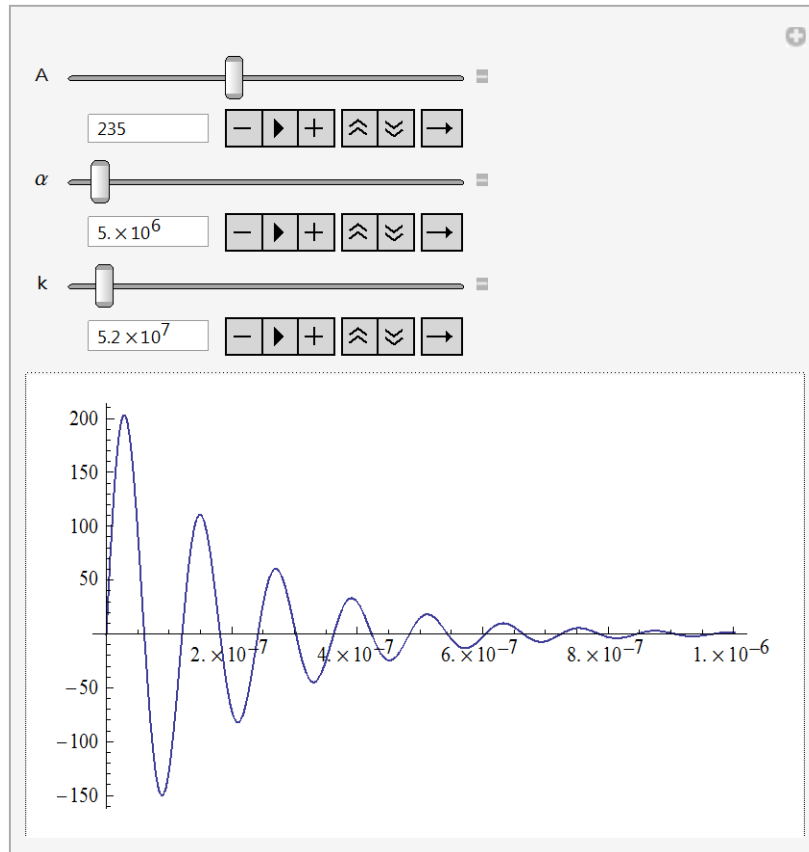


Now use the manipulate function to examine the data set. Start by guessing a functional form, and plot the functional form over a range of fit parameters (Amplitude and wave number).

Then, change the fit parameters to get the form to match the data set.

```
fGuess[A_,k_,α_,t_]:=A e-α t Sin[k t]

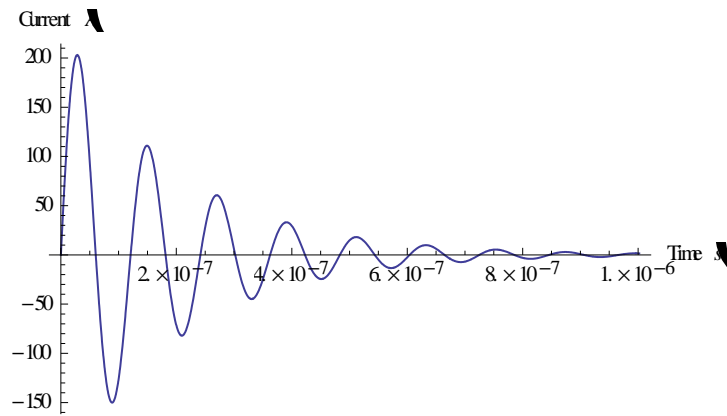
Manipulate[Plot[fGuess[A,k,α,t],{t,0,Max[plotData[[All,1]]]},PlotRange→All],{
A,50,500},{α,106,108},{k,106.5,109}]
```



Now set values for the fit parameters, based on what was found above, and plot the fit function over the range of x-values from the imported data.

```
Afit=235;
kfit=5.2 107;
αfit=5.0 106;
tmin=Min[plotData[[All,1]]];
tmax=Max[plotData[[All,1]]];
```

```
fitPlot=Plot[fGuess[Afit,kfit, $\alpha$ fit,t],{t,tmin,tmax},PlotRange→All,AxesLabel→{Time[s], Current[A]}
```

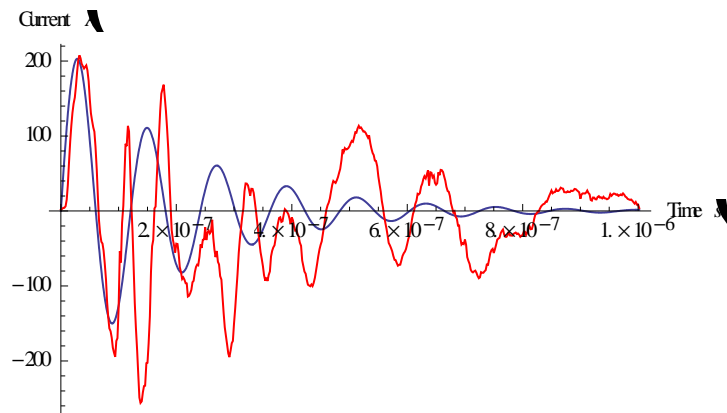


```
freq=N[kfit/(2 $\pi$ )]
```

8.27606×10^6

Show both plots together.

```
Show[fitPlot,dataPlot,AxesLabel→{Time[s], Current[A]}]
```



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